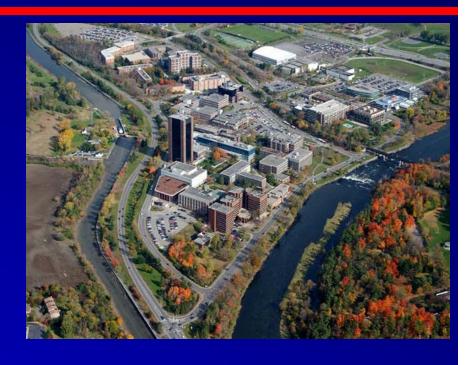
## Some recent dosimetry studies with EGSnrc

D. W. O. Rogers,
Carleton Laboratory for
Radiotherapy Physics,
Physics Dept,
Carleton University,
Ottawa



http://www.physics.carleton.ca/~drogers AIFM Workshop, Rome, May 23, 2009





## P<sub>repl</sub>: PhD work of Lilie L W Wang



"Study of the replacement correction factors for ionization chamber dosimetry by Monte Carlo simulation"

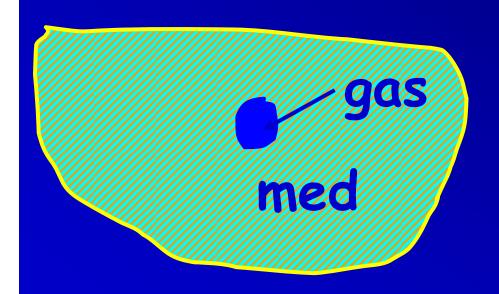
Carleton University, **April** 2009 Nominated for a Senate Medal Many slides are from his work



See http://www.physics.carleton.ca/~drogers/pubs/theses and 7 publications referenced therein (on line same site) 2/44

# Cavity theory: stopping-power ratios

Relates dose in cavity to dose in medium.

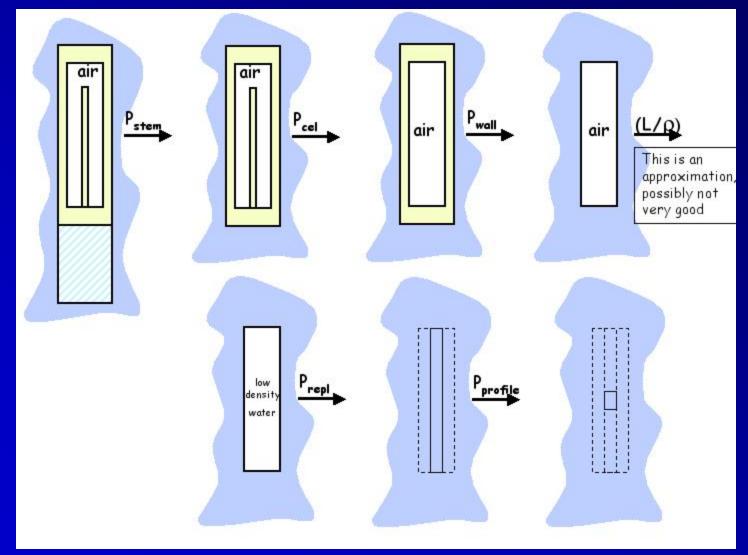


sprs are fundamental to
-dosimetry protocols
-primary standards

$$D_{med} = D_{gas} \left( \overline{L}/
ho 
ight)_{gas}^{med}$$



# Dosimetry in a water tank with realistic ion chamber





#### Dosimetry in a water tank

$$D_{ ext{med}} = D_{ ext{gas}} \left(rac{L}{
ho}
ight)_{ ext{air}}^{ ext{med}} P_{ ext{wall}} P_{gr} P_{fl} P_{ ext{cel}}$$

$$P_{
m repl} = P_{gr} P_{fl} = p_{
m dis} p_{
m cav}$$

for complete definitions of  $P_{wall}$  etc see http://www.physics.carleton.ca/~drogers/pubs/papers/ss96.pdf



## P<sub>repl</sub> in dosimetry protocols

#### Electron beams

- "well-guarded" plane-parallel chambers: P<sub>repl</sub> = 1
- cylindrical chambers: measured  $P_{repl}$  at  $d_{max}$  (=  $P_{fl}$ )

#### Photon beams

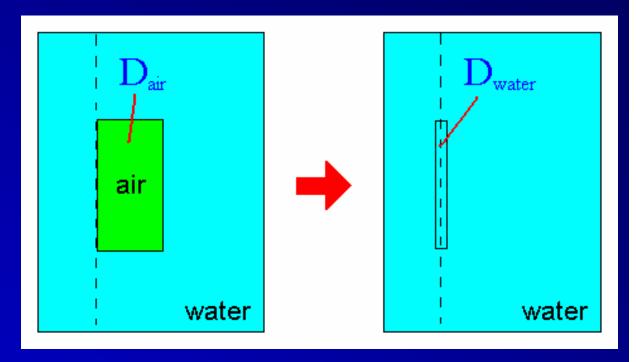
- plane-parallel chambers: P<sub>repl</sub> = 1
- cylindrical chambers: measured P<sub>repl</sub> = P<sub>gr</sub>

TRS-398: the uncertainty in value of  $P_{repl}$  in photon beams "is one of the major contributions to the final uncertainty in  $k_0$ "



## P<sub>repl</sub> calculation methods (I)

#### SPR method



$$P_{ ext{repl}} = \left. rac{D_{ ext{water}}}{D_{ ext{air}}} \middle/ \left( rac{\overline{L_{\Delta}}}{
ho} 
ight)_{ ext{air}}^{ ext{water}}$$



Need a separate stopping-power ratio calculation.
This is "traditional" technique - residual effect

## P<sub>repl</sub> calculation methods (II)

#### FLU method

If electron fluence spectrum in air cavity differs from that in water only by a constant, i.e.  $\Phi_{\text{water}}(E) = \text{const} \times \Phi_{\text{air}}(E)$ , then

$$P_{ ext{repl}} = rac{\Phi_{ ext{Total,water}}}{\Phi_{ ext{Total,air}}}$$



P<sub>repl</sub> value depends on the above assumption

## P<sub>repl</sub> calculation methods (III)

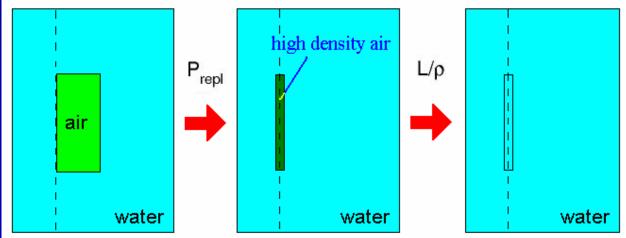
#### HDA method

(direct method)

$$P_{ ext{repl}} = \left. rac{D_{ ext{HDA}}}{D_{ ext{air}}} \middle/ \left( rac{\overline{L_{\Delta}}}{
ho} 
ight)_{ ext{air}}^{ ext{air}}$$



$$P_{ ext{repl}} = rac{D_{ ext{HDA}}}{D_{ ext{air}}}$$



Replace thin slab of water with thin slab of high density air (HDA) which is same as normal-density air except with water density.

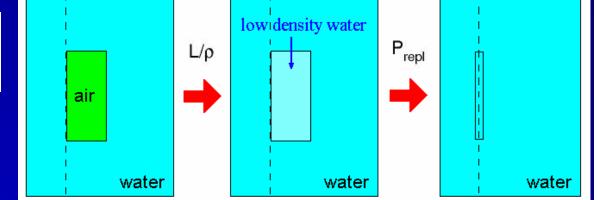


## P<sub>repl</sub> calculation methods (IV)

#### LDW method

(direct method)

$$P_{ ext{repl}} = rac{D_{ ext{water}}}{D_{ ext{LDW}}}igg/\left(rac{\overline{L}_{\Delta}}{
ho}
ight)_{ ext{water}}^{ ext{water}}$$





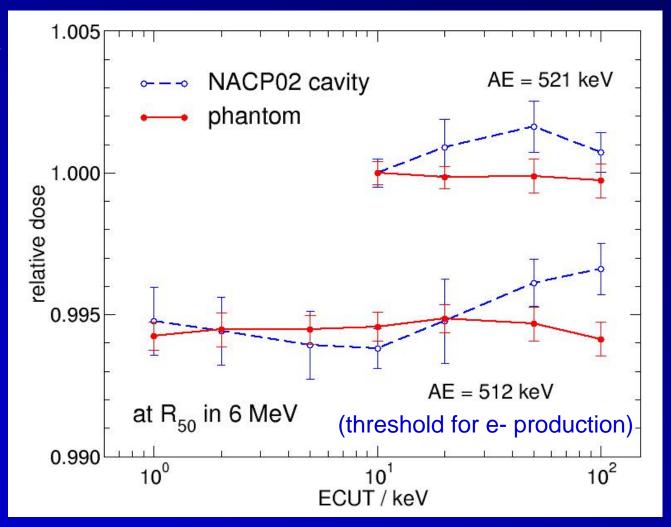
$$P_{ ext{repl}} = rac{D_{ ext{water}}}{D_{ ext{LDW}}}$$

Replace air in cavity with low density water (LDW) which is same as normal-density water except with air's density



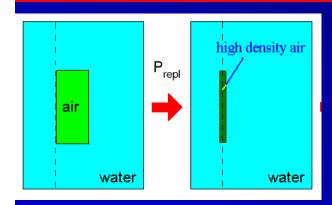
## Dose in water & NACP02 cavity vs cutoff energy at $R_{50}$ in 6 MeV electron beam

- difference due to energy-loss straggling effects on depth-dose
- but ratio
  independent of
  AE or ECUT at
  0.1% stats
- AE 512 3-5 times slower





#### HDA method: uncertainties

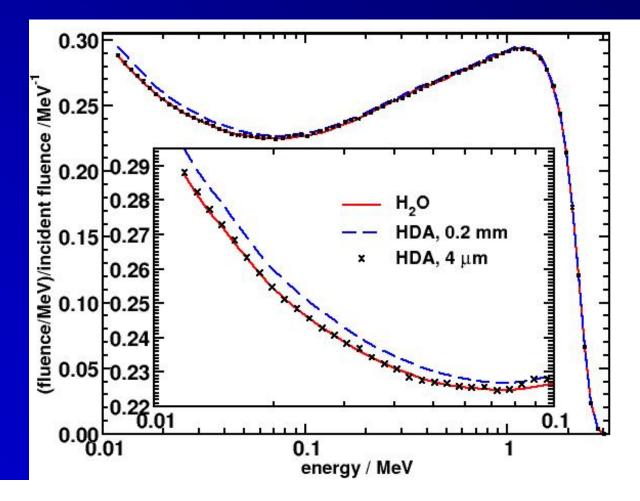


Assumption is that spectra in HDA and water are the same

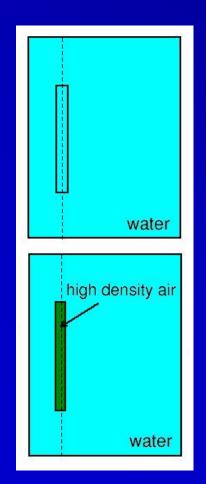
-if slab
sufficiently thin.

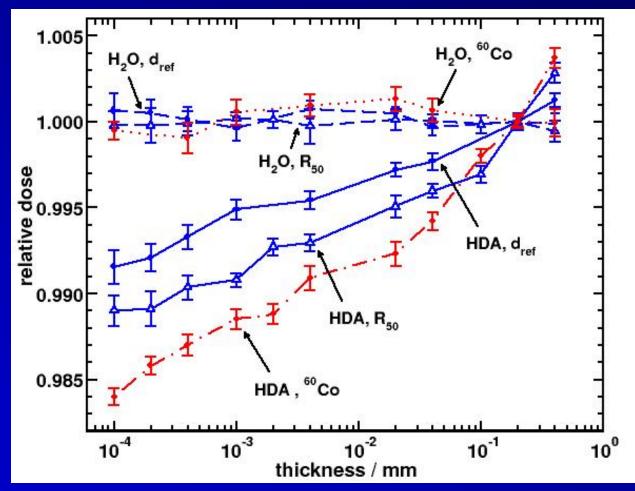


$$P_{ ext{repl}} = rac{D_{ ext{HDA}}}{D_{ ext{air}}}$$



#### HDA method: slab thickness

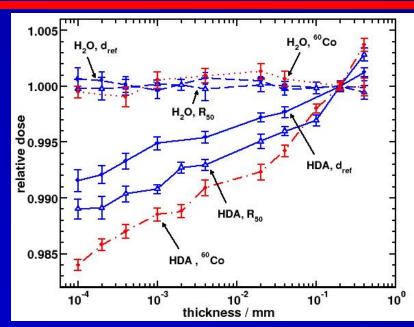






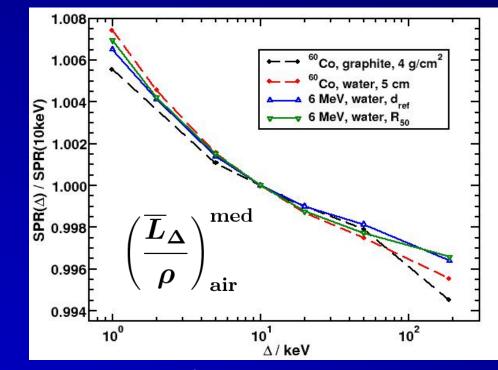
Is the variation due to fluence perturbation or? Constant  $H_2O$  result => OK with very thin slabs.

#### HDA method: slab thickness



At least part of the variation is due to variation in  $\Delta$  which is related to thickness via range of e-

$$rac{D_{\mathrm{water}}}{D_{\mathrm{HDA}}} = \left(rac{\overline{L}_{\Delta}}{
ho}
ight)_{\mathrm{air}}^{\mathrm{water}}$$





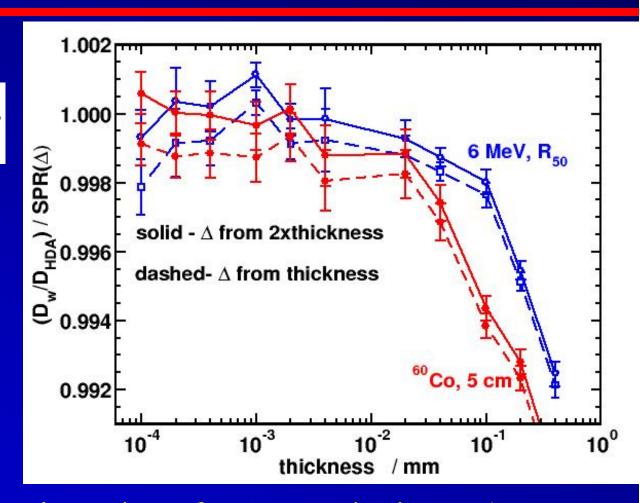
Select thickness corresponding to cavity average chord via L=4V/S = 2t, or just t

### HDA: is there a perturbation?

#### If yes, then:

$$rac{D_{\mathrm{water}}}{D_{\mathrm{HDA}}} = \left(rac{\overline{L}_{\Delta}}{
ho}
ight)_{\mathrm{air}}^{\mathrm{water}} P$$

Dose ratio/spr constant (=1) => no fluence perturbation. For greater thickness there is (seen at 2 mm above).



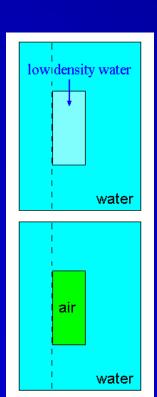


2 possible algorithms for D, 2xthickness better
But difference less than 0.2%

# Uncertainty of $P_{repl}$ : perturbation of electron fluence in LDW cavity

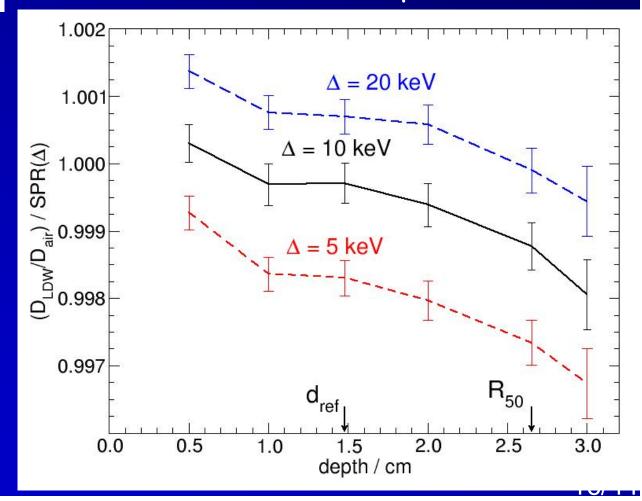
$$rac{D_{ ext{LDW}}}{D_{ ext{air}}} = \left(rac{\overline{L}_{\Delta}}{
ho}
ight)_{ ext{air}}^{ ext{LDW}} P$$

NACP02
cavity in
a 6 MeV
e- beam
vs
depth





If there is no perturbation, then ratio of doses/spr = 1.0



## P<sub>repl</sub> at 10 cm depth in water: 60 Co

Under Fano conditions (no attenuation or scatter), P<sub>repl</sub> should be unity if the method is working.

cavity radius	$0.5 \mathrm{\ mm}$	$3 \mathrm{\ mm}$	5 mm
$P_{\text{repl}}$ (normal)	0.9979(7)	0.9961(5)	0.9939(4)
$P_{\text{repl}}$ (Fano)	0.9991(7)	0.9993(6)	0.9997(6)



## P<sub>repl</sub>: Overall uncertainty

- statistics can be well less than 0.1%
- -HDA technique, select thickness of HDA corresponding to  $\Delta$  appropriate for cavity. 1.3 to 3  $\mu$ m typically.
- -for low Z, => < 0.2% uncertainty
- -for high  $Z \Rightarrow$  large uncertainty since variation in  $D_{HDA}$  with thickness is much larger
- -LDW method uncertainty about same due to inability to demonstrate the lack of fluence perturbation between air and LDW



# P<sub>repl</sub> for NACP02 chamber in electron beams and <sup>60</sup>Co beam

Calculation is done at  $d_{ref}$  for electron beams & at depth 5 cm for  $^{60}\text{Co}$  beam

	SPR	FLU	HDA	LDW
6 MeV	0.9956 (0.06%)	0.9977 (0.10%)	0.9976 (0.08%)	0.9959 (0.06%)
18 MeV	1.0001 (0.06%)	1.0007 (0.06%)	1.0011 (0.07%)	1.0005 (0.05%)
60 <mark>Co</mark>	1.0059 (0.10%)	1.0063 (0.10%)	1.0062 (0.10%)	1.0065 (0.10%)



In all dosimetry protocols:  $P_{repl} = 1$ 

#### P<sub>repl</sub> for Farmer chamber in <sup>60</sup>Co beam

Cavity diameter: 6 mm

Cavity length: 2 cm

Depth in water: 5 cm

SPR	FLU	HDA	LDW
0.9963	0.9952	0.9969	0.9974
(0.08%)	(0.08%)	(0.09%)	(0.07%)

#### P<sub>repl</sub> value in dosimetry protocols:

AAPM 0.992 IAEA 0.988



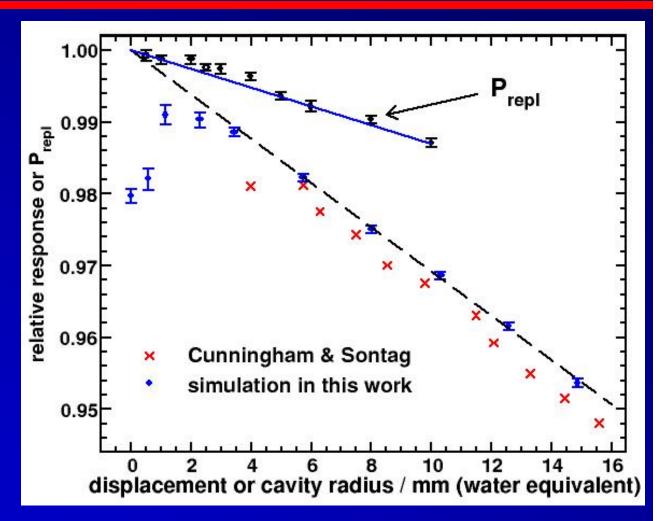
## P<sub>repl</sub> for photon beams (AAPM)

TG-21/TG-51 use values based on measurements by Cunningham and Sontag (1980)

The MC values differ considerably but duplicated the original measurements.

#### Conclusion:

Original interpretation of measurements in terms of P<sub>repl</sub> was incorrect.





## P<sub>repl</sub> for photon beams (IAEA)

IAEA uses values of Johansson et al (1977).

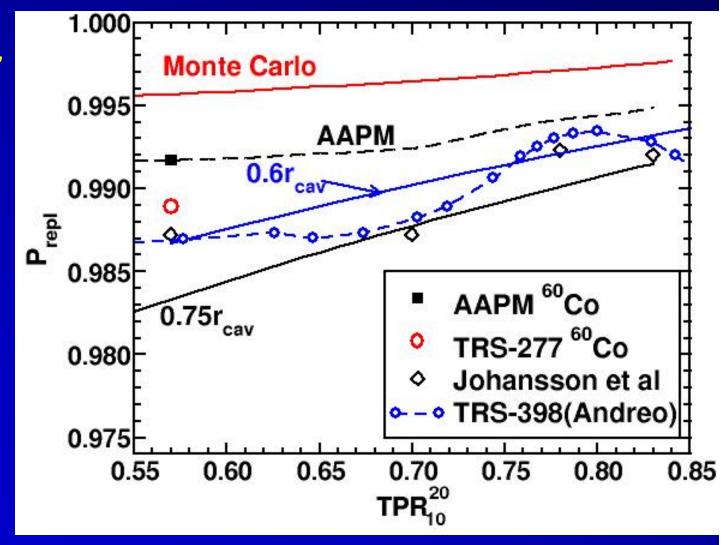
- -values even farther from the Monte Carlo values
- problem was way in which the data were normalized between chambers with different radii
- using their normalization Monte Carlo of the experiment matches their results
- using correct normalization Monte Carlo of their experiment yields same result as Monte Carlo of  $P_{\text{repl}}$



# P<sub>repl</sub> for Farmer chamber in photon beams

#### Lower two lines

Equivalent from effective point of measurement as labelled



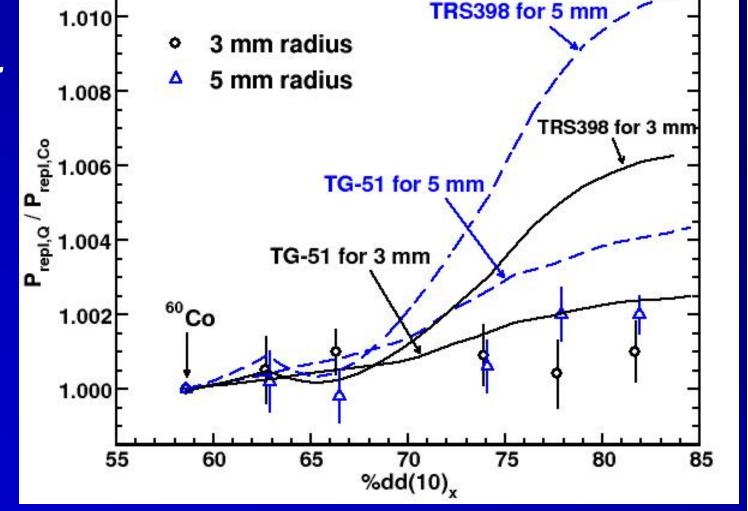


## The ratio of P<sub>repl</sub> in a photon beam to that in a <sup>60</sup>Co beam vs beam quality

#### Good news

It is only this ratio that matters in TG-51 & TRS-398

Difference not as much as absolute value



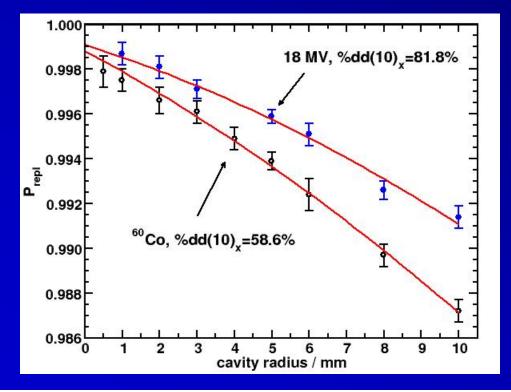
24/44



## P<sub>repl</sub> in photon beams

$$egin{array}{lll} P_{repl} &=& 0.9974 - 0.00183 \; r + 3.36 imes 10^{-5} \; \% dd (10)_x - 2.7 imes 10^{-5} \; r^2 \ &- 1.6 imes 10^{-7} \; (\% dd (10)_x)^2 + 1.58 imes 10^{-5} \; r \; \% dd (10)_x, \end{array}$$

$$egin{array}{lll} P_{repl} &=& 1.0021 - 0.00188 \ r - 0.0108 \ TPR_{10}^{20} - 2.5 imes 10^{-5} \ r^2 \ &+ 0.009 \ (TPR_{10}^{20})^2 + 0.00169 \ r \ TPR_{10}^{20}, \end{array}$$





### The Value of (W/e)air

(W/e)<sub>air</sub> plays a central role in radiation dosimetry

It links the charge measured to the dose

$$D_{
m air} = \left(rac{W}{e}
ight)_{
m air} rac{Q}{m_{
m air}}$$

$$N_{
m gas} = N_D = rac{\left(rac{W}{e}
ight)_{
m air}}{m_{
m air}}$$

 $(W/e)_{air}$  drops out of TG-51/TRS-398 on the assumption it is a constant.

BUT the world's air kerma standards are all directly proportional to its value



### Measuring (W/e)air

In graphite determine  $D_{gr}$  using a calorimeter.

Then using a graphite-walled ion chamber, measure the absorbed dose using an ion chamber

$$D_{gr} = rac{Q}{m_{
m air}} \left(rac{W}{e}
ight)_{
m air} \left(rac{\overline{L_\Delta}}{
ho}
ight)_{
m air}^{
m gr} P_{
m repl}$$

Experiment actually extracts the product (W/e).spr

Result directly linked to P<sub>repl</sub> value

Niatel et al, PMB 30(1985) 67-75



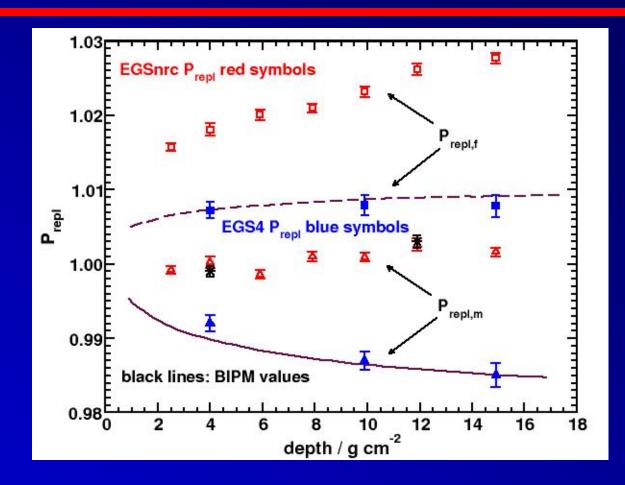
## Calculations of P<sub>repl</sub>

Two values

-point of measurement

-at front-at mid-plane

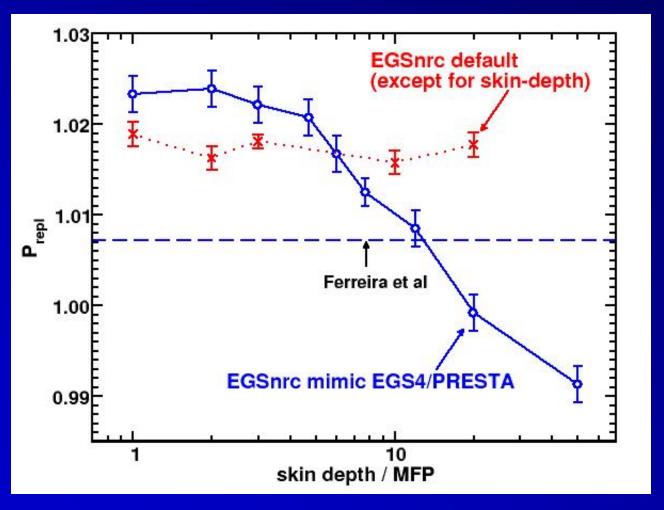
EGS4 Ferreira et al 43 (1998) 2721



BIPM calns for  $K_{an}$  based on same techniques have been shown incorrect for  $K_{an}$ 



#### EGS4 vs EGSnrc calculations





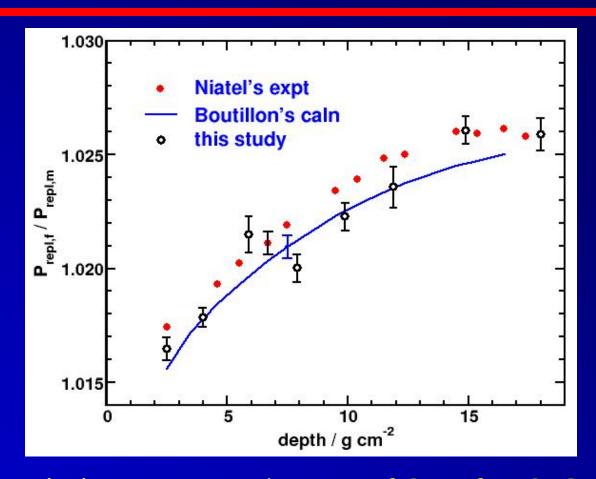
EGS4: Ferreira et al 43 (1998) 2721

## P<sub>repl</sub> experimental verification

measured ratios for

front/mid-plane values vs depth

Both calculations agree.





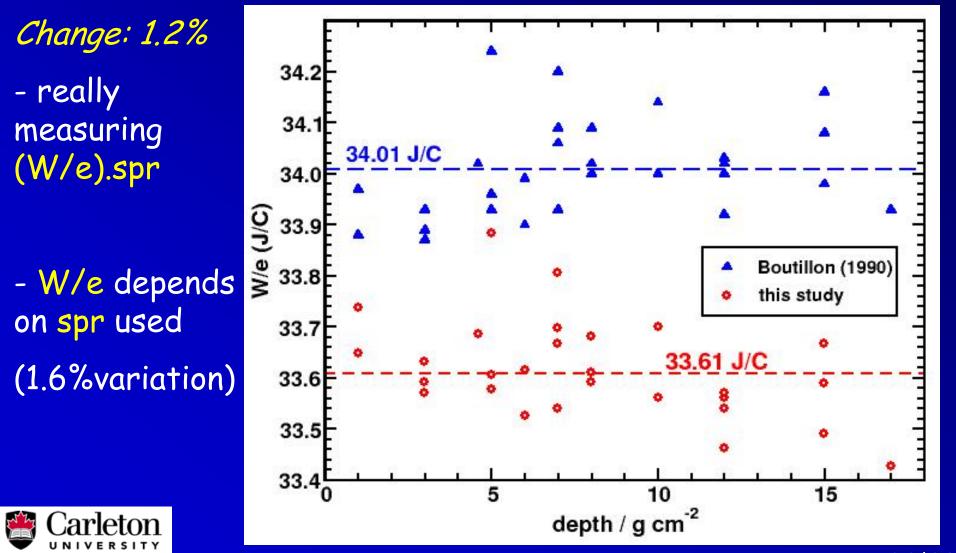
Ferreira et al also measured ratio of  $P_{repl}$  for BIPM & IRD chambers vs depth and our calculated results agree with the measurements.

### (W/e) from multiple calorimeter

Change: 1.2%

- really measuring (W/e).spr

(1.6%variation)





#### W/e value: Niatel et al

Niatel et al used another method to measure

- using the measured activity they calculated the collision air kerma
- they took the measured exposure rate and divided by  $(W/e)_{air}$  to get the collision air kerma
- -solve resulting equations for (W/e)air.spr
- (W/e)<sub>air</sub>.spr is inversely proportional to exposure
- original 33.81 J/C +-0.42% becomes 33.61+-0.23%



#### W/e value: Niatel et al

Calorimetric method: new Prepl

34.01 J/C --> 33.61 J/C

Exposure/activity method: new exposure standard 33.81 J/C --> 33.61 J/C

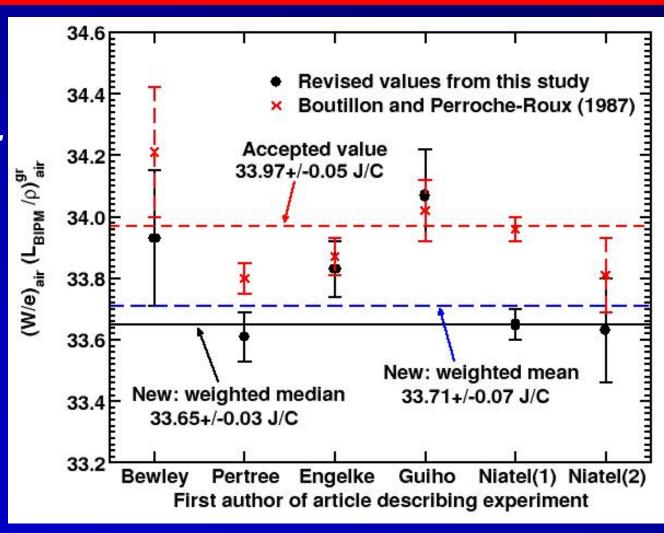
But really measuring product  $(W/e)_{air}$  spr and the spr  $(L/\rho)_{gr,air}$  is uncertain



### W/e.spr value: reanalysis

6 experiments contribute to the value of this product

Re-analyzed all (not all used wrong value of P<sub>repl</sub>)





Rowan Thomson, in preparation

### W/e.spr value: reanalysis

33.97 (5) J/C --> 33.65 (3) J/C 0.95% change from a value with stated uncertainty of 0.15%

Implies world's air kerma standards for 60Co will need to be reduced by 0.95%.

Implications for W/e value (without spr) unclear until issue of the best value of  $(L/\rho)_{gr,air}$  is resolved



## Determining effective point of measurement: matching depth-ionization curves

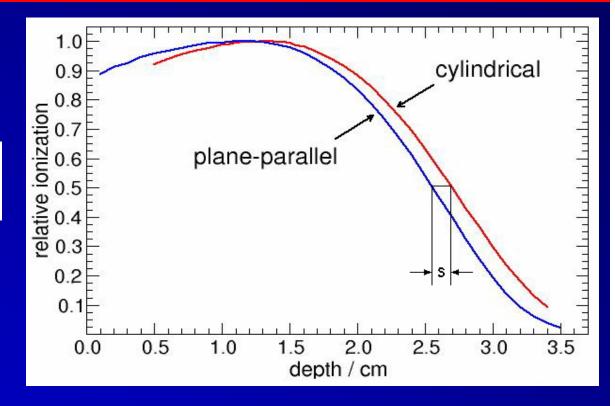
Use calculated depth-ionization curve

$$D_{\mathrm{water}} = D_{\mathrm{air}}^{\mathrm{ideal}} \left(rac{\overline{L}_{\Delta}}{
ho}
ight)_{\mathrm{air}}^{\mathrm{water}}$$

Vary the offset s

$$z_i = z_{0,i} + s$$

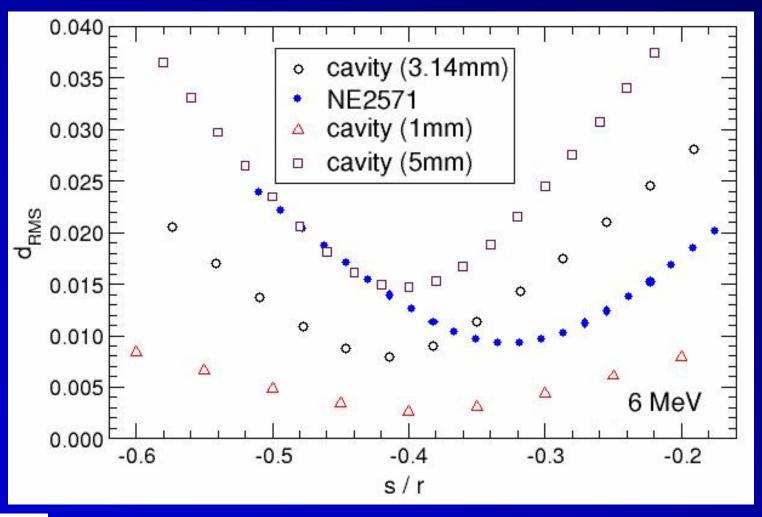
to minimize d(s)



$$d(s) = \sqrt{rac{\sum_i \left[D_{\mathrm{air}}^{\mathrm{ideal}}(oldsymbol{z}_i) - lpha \cdot D_{\mathrm{air}}(oldsymbol{z}_{0,i})
ight]^2}{N}}$$

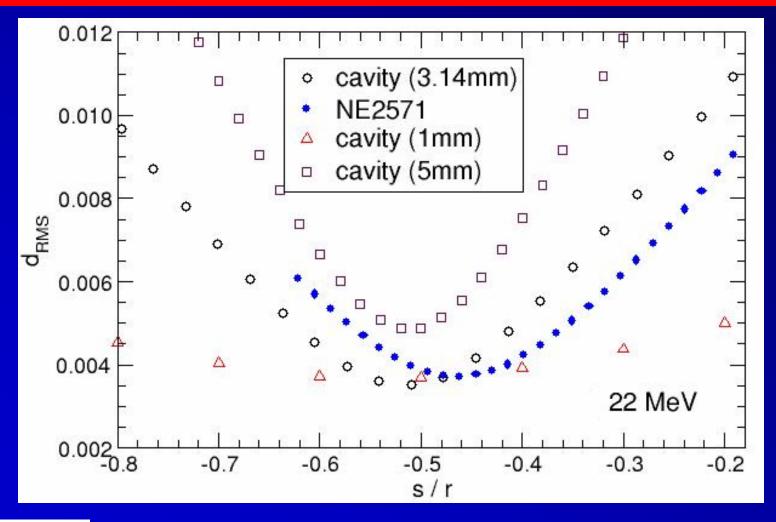


## Shift for cylindrical chamber in 6 MeV electron beam



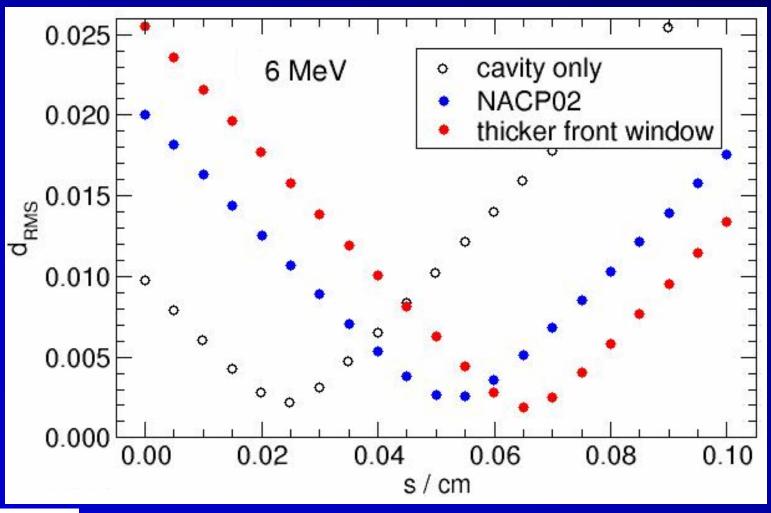


# Shift for cylindrical chamber in 22 MeV electron beam



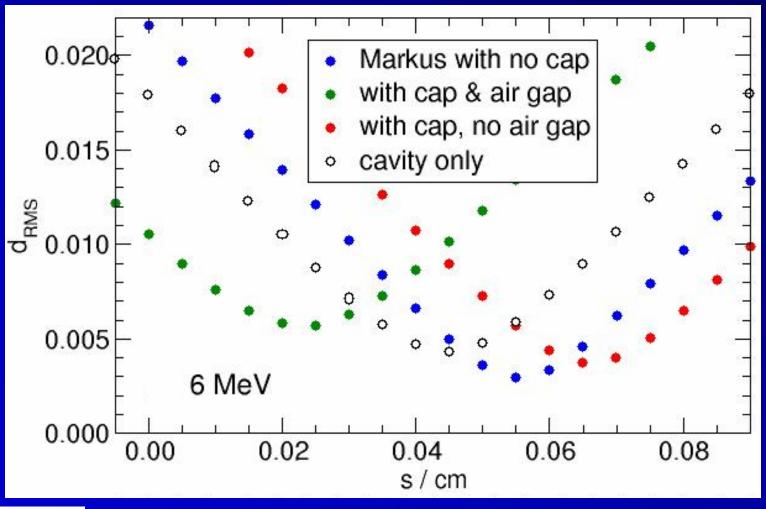


# Shift for NACP02 chamber in 6 MeV electron beam





# Shift for Markus chamber in 6 MeV electron beam

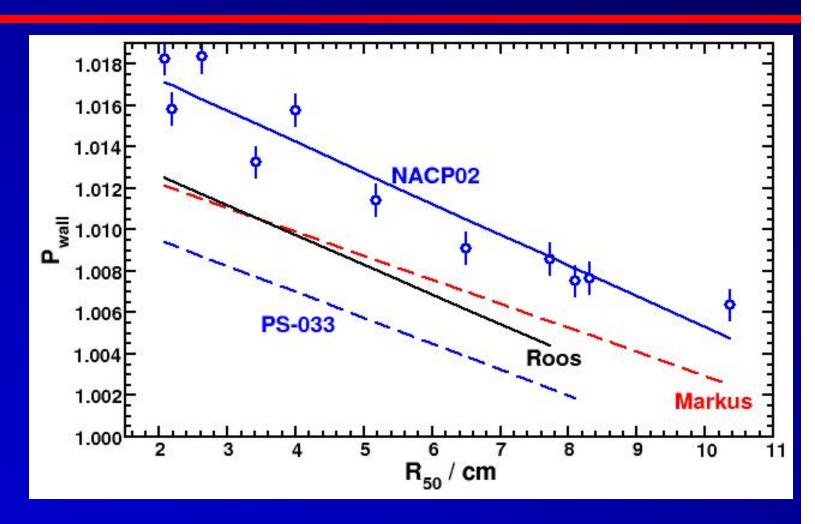




# P<sub>wall</sub> for plane-parallel chambers in electron beams

protocols currently all use P<sub>wall</sub>=1.0

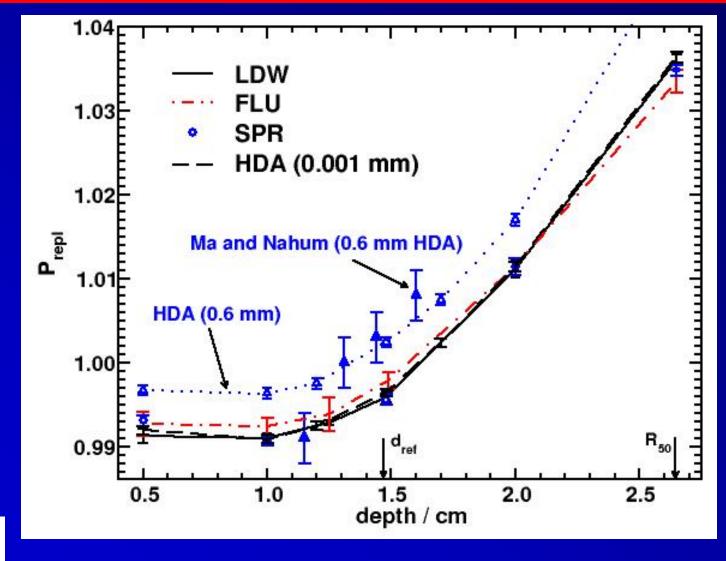
for all planeparallel chambers





Buckley & Rogers, Med. Phys. 33(6), 1788 (2006)

#### P<sub>repl</sub> vs depth for NACP02 chamber in 6 MeV electron beam





#### Conclusions

- Monte Carlo calculations can contribute to ion chamber dosimetry
- P<sub>repl</sub> values for plane-parallel chambers are not unity in electron beams as assumed in protocols
- effective point of measurement is not exactly the front of the cavity for plane-parallel chambers in electron beams and is close to the centre of the cavity in photon beams
- values of (W/e)<sub>air</sub>.spr need to be revised downwards by 6 times their stated uncertainty



#### Acknowledgements

- the work reported on here is almost entirely from the PhD work of Lilie Wang http://www.physics.carleton.ca/~drogers/pubs/theses
- the work of Rowan Thomson and Lesley Buckley was also referred to.
- Work supported by the Canada Research Chairs program, an OGS scholarship (for LLW Wang) and





