The Use of EGS for Monte Carlo Calculations in Medical Physics

D.W.O. Rogers and A.F. Bielajew Physics Division, National Research Council of Canada Ottawa, Canada KIA OR6 (613) 993-2715 or 993-2197

Lecture notes for Refresher Course RC7 First Inter-American Meeting of Medical Physics Chicago, July 17 1984

> Report PXNR-2692 June, 1984

The Use of EGS for Monte Carlo Calculations

in Medical Physics

Refresher Course RC7

First Inter-American Meeting of Medical Physics

Tuesday, July 17, 1984, Chicago

SLIDE 2

Course Outline

- 1) Introduction to EGS
- 2) Why Use EGS

3) A Simple Example of its Use

- 4) Parameter Selection
- 5) Variance Reduction Techniques
- 6) Benchmarks

Notes: The course assumes a basic familiarity with the Monte Carlo technique of radiation transport. The emphasis will be on the use of EGS to do medical physics related calculations in which electron transport is important. However, many of the considerations are valid with other codes.

Introduction to EGS

(Electron-Gamma-Shower)

Version 3: Developed at SLAC for High Energy Physics Applications

Version 4: Modified & corrected for applications down to 100 keV.

Uses condensed history technique of charged particle transport

Highly Structured and General Purpose

Written in an extended Fortran called MORTRAN

Notes: See Ford and Nelson,1978 and Nelson et al 1984, for detailed documentation or Rogers 1982,1984a,1984b for briefer descriptions. Write to Dr.W.R.Nelson, Stanford Linear Accelerator Center, P.O.Box 4349, Stanford CA94305 for SLAC report 210.

SLIDE 4

The Physics in the Simulation

Electron/Positron Transport

Photon Transport

Compton Scattering

Bremsstrahlung Production (no Elwert correction)

Positron annihilation in flight and at rest

Moliere Multiple Scattering (coulomb scatter from nuclei)

Moller & Bhabha Scattering (scattering from electrons) Rayleigh(coherent)Scattering (Version 4 only)

Photo-electric effect (K x-rays not followed)

Pair Production

Continuous energy loss (restricted Bethe-Bloch)

Notes: Ford and Nelson, 1978 give very clear and complete documentation.



Notes: The user writes a users code to handle input and output, to do a statistical analysis of the results and to call, via a simple subroutine call, the EGS system to do the actual radiation transport simulation. The user also supplies two subroutines called HOWFAR and AUSGAB. HOWFAR basically specifies the users geometry and answers a few very specific questions. AUSGAB keeps track of the parameters of interest. It can be very simple or very sophisticated. It is called under a set of very well defined and selectable conditions (e.g. at the beginning of every electron step) and the user has access to a set of well defined parameters (e.g.position, direction, energy, energy deposited and pathlength traversed in this step etc).

The cross-secton preparation code called PEGS is much larger than EGS. It can prepare data sets for materials of arbitrary composition.

SLIDE 6

Why Use EGS?

- 1) Very Flexible can handle virtually any problem
- 2) More accurate and easier than writing your own routines
- 3) Well documented and benchmarked you specify what you have done by using a standard code.
- 4) Your improvements and error corrections are a general contribution to the field.

Notes: The major competitor to EGS is Berger and Seltzer's ETRAN and its Sandia Labs extentions (CYLTRAN, ACCEPT, SANDYL). These codes are perhaps more sophisticated than EGS in their low energy electron transport and represent a benchmark for EGS. However ETRAN is not flexible (except for Berger and Seltzer!) and cannot be applied by others to problems other than those it is designed for. Its published documentation is poor although the range of published benchmark comparisons to experiment is still better than for EGS.



Notes: These results are for a fairly thin target; 95% of the electrons go through and exit with an average energy of 14.3 MeV. ECUT=AE=1.5 MeV(total energy), AP=PCUT=0.100 MeV, default ESTEPE.

```
SLIDE 8
```

```
.
                         AN UNCOMMENTED VERSION OF AAPM.MOR
0
            AAPMS . MOR
   701
   %C80
   %'$MXMED'='1' %'$MXREG'='3' %'$MXSTACK'='15'
   %';COMIN/GEOM/;'=';COMMON/GEOM/ZBOUND;'
   $COMIN/BOUNDS,GEOM,MEDIA,THRESH/;
0
   INTEGER MEDARR(24) /$S'TA',22*' '/; DO I=1,24<MEDIA(I,1)=MEDARR(I);>
0
0
   ZBOUND=0.1;
                    START AAPM'//' CALL HATCH TO GET CROSS-SECTION DATA'/);
   ;OUTPUT;(///'
0
0
   CALL HATCH;
   JOUTPUT AE(1)-0.511, AP(1); ('OELECTRONS CAN BE CREATED OR FOLLOWED DOWN TO',
Ō
   F8.3,' MeV KINETIC ENERGY'/' PHOTONS CAN BE CREATED OR FOLLOWED DOWN TO',
0
0
   F8.3,' MeV ');ECUT(2)=1.5;PCUT(2)=0.1;
0
   iOUTPUT;('0',T19,'KINETIC ENERGY(MeV)',T40,'CHARGE',T48,
   'ANGLE W.R.T. Z AXIS-DEGREES'); IQIN=-1; EIN=20,511; /XIN, YIN, ZIN/=0.0;
0
   /UIN,VIN/=0.0;WIN=1.0;IRIN=1;WTIN=1.0;INRCIN=0;
0
   DO I=1,10<OUTPUT I;(' START HISTORY', I4);
0
        CALL SHOWER(IQIN, EIN, XIN, YIN, ZIN, UIN, WIN, WIN, IRIN, WTIN, INRCIN);>
1
   STOP; END;
0
   SUBROUTINE AUSGAB(IARG);
0
    COMIN/STACK/; IF(IARG.EQ.3) <ANGLE=ACOS(W(NP))*180./3.14159;
0
        IF(IQ(NP),EQ.0)<EKINE=E(NP);> ELSE <EKINE=E(NP)-0.511;>
1
        OUTPUT EKINE, IQ(NP), ANGLE; (T21, F10, 3, T33, I10, T49, F10, 1);>
1
0
   RETURN; END;
0
   SUBROUTINE HOWFAR;
0
    COMIN/STACK, EPCONT, GEOM/;
0
   IF(IR(NP),EQ,3)<IDISC=1;RETURN;>
0
    ELSEIF(IR(NP).EQ.2)<IF(W(NP).GT.0.0)<
2
            TVAL=(ZBOUND-Z(NP))/W(NP); IF(TVAL.GT.USTEP)<RETURN;>
2
            ELSE<USTEP=TVAL $ IRNEW=3 $ RETURN $>>
1
        ELSEIF(W(NP)+LT+0+0)<TVAL=-Z(NP)/W(NP);IF(TVAL+GT+USTEP)<RETURN;>
2
            ELSE<USTEP=TVAL # IRNEW=1 # RETURN #>>>
1
        ELSEIF(W(NP),EQ.0.0)<RETURN;>>
  ELSEIF(IR(NP),EQ.1)<IF(W(NP),GT.0.0)<USTEP=00.00;IRNEW=2;RETURN;>
0
1
        ELSE<IDISC=1;RETURN;>>
0
    END;
    %Q0
    7%
```

Notes: This code + the EGS system does all the physics shown in slide 7, although it does not analyse the results. Its output is shown in the next slide. A commented version is given in slides 10,11,12. This version is presented to emphasize how simple it is to do physics with the EGS system.

@AAPM \$ASSIGN NL: FOR008 \$ASSIGN EDAVE.PEGS.DATJEGSHI.DAT FOR012 \$ASSIGN TT: FOR006 \$RUN AAPM

START AAPM

CALL HATCH TO GET CROSS-SECTION DATA

ELECTRONS CAN PHOTONS CAN	BE CREATED OR FOLLOWED BE CREATED OR FOLLOWED	DOWN TO DOWN TO	0.989 MeV KINETIC ENERGY 0.100 MeV
START HISTORY	KINETIC ENERGY(MeV)	CHARGE	ANGLE W.R.T. Z AXIS-DEGREES
	0.284	0	23.2
	1+652	0	28.0
	15.870	-1	25.0
START HISTORY	2		
	0.544	0	2.7
	0.573	0	22.5
	16.800	-1	19,6
START HISTORY	3		
	0.196	0	5.2
	5,194	0	18.8
	0.133	0	14.1
	12,400	-1	17.3
START HISTORY	4		
	0,339	0	4.4
	0.895	0	11.1
	16,708	-1	19.6
START HISTORY	5		
	0.704	0	3.1
	17,253	-1	6+8
START HISTORY	6		
	17.911	0	19.9
START HISTORY	7	*	
	0.561	0	16.9
	0.113	0	17.5
	17,249	-1	31.8
START HISTORY	8		
	17.746	-1	55.7
START HISTORY	9		
	5.878	-1	22+5
	11.968	0	1.1
START HISTORY	10		
	0.701	0	81.0
	17.142	0	3.7
FORTRAN STOP			
\$			

Note: Total CPU time for the simulation was 150ms on a VAX 780.

```
SLIDE 10
   701
   2C80
           USE 80 COLUMNS
    0
0
                                 ******
0
    .
0
                                 *
                                          *
    .
0
                                 * AAPM.MOR*
0
                                 *
                                          *
0
    .
                                 *****
0
    .
0
           An EGS program which lists the particles escaping from
0
    .
           a 1 mm thick slab of Ta onto which a 20 MeV pencil beam of electrons
0
    в
           has been directed
    H.
0
    .
0
           Dave Rosers Feb 1984, NRCC
0
0
    0
0
    "set some user defaults
0
    %'$MXMED'='1' "There is only 1 medium in the problem
    %'$MXREG'='3' There are only 3 geometric regions (defaults 2000)
                        "less than 15 particles on the stack at once
    %'$MXSTACK'='15'
0
    "DEFINE A COMMON TO PASS INFORMATION TO THE GEOMETRY ROUTINE HOWFAR
0
    %' COMIN/GEOM/;'=';COMMON/GEOM/ZBOUND;'
0
    ;COMIN/BOUNDS,GEOM,MEDIA,THRESH/; NOTE WE NEED A ; TO START THE FIRST REAL LINE
0
           BOUNDS CONTAINS ECUT AND PCUT
0
    .
           GEOM PASSES INFO TO OUR HOWFAR ROUTINE
0
    8
           MEDIA CONTAINS THE ARRAY MEDIA
0
    8
           THRESH CONTAINS AE AND AP
0
0
    INTEGER MEDARR(24) /$S'TA',22*' '/; "PLACE MEDIUM NAME IN AN ARRAY
0
    DO I=1,24<MEDIA(I,1)=MEDARR(I);>"THIS IS TO AVOID A DATA STATEMENT FOR
0
                                    A VARIABLE IN COMMON
0
    ZBOUND=0.1;" plate is 1mm thick
0
0
    fourfulf;(///' START AAPM'//' CALL HATCH TO GET CROSS-SECTION DATA'/);
0
0
                  PICK UP CROSS SECTION DATA FOR TA
0
    CALL HATCH; "
                   DATA FILE MUST BE ASSIGNED TO UNIT 12
 0
0
    ;OUTPUT AE(1)-0,511, AP(1); ('OELECTRONS CAN BE CREATED OR FOLLOWED DOWN TO',
0
    F8.3,' MeV KINETIC ENERGY'/' PHOTONS CAN BE CREATED OR FOLLOWED DOWN TO',
 0
    F8.3,' MeV ');
0
                  TERMINATE ELECTRON HISTORIES AT 1.5 MEV IN THE PLATE
 0
    ECUT(2)=1.5;*
    PCUT(2)=0.1;* TERMINATE PHOTON HISTORIES AT 0.1 MEV IN THE PLATE
 0
 0
    7E
Notes:i)Variables in common are carefully documented in SLAC 210.
ii) The numbers down the left indicate the current level of nesting, and are
matched by automatic indentation (all level 0 here).
iii) ; ends all statements
iv) OUTPUT writes to unit 6 with the format following it.
v) %'TEXT1'='TEXT2' defines a macro substitution. This replaces all occurances
```

2

of TEXT1 by TEXT2. It is used here to define some dimensions.

0 *PRINT HEADER FOR OUTPUT 0 fOUTFUT;('0',T19,'KINETIC ENERGY(MeV)',T40,'CHARGE',T48, 'ANGLE W.R.T. Z AXIS-DEGREES'); 0 0 0 "DEFINE INITIAL VARIABLES FOR 20 MEV BEAM OF ELECTRONS NORMALLY INCIDENT 0 "ON THE SLAB 0 IQIN=-1;" INCIDENT CHARGE - ELECTRONS 0 EIN=20.511;* 0 20 MEV KINETIC ENERGY /XIN,YIN,ZIN/=0.0;" 0 INCIDENT AT ORIGIN 0 /UIN,VIN/=0.0;WIN=1.0;" MOVING ALONG Z AXIS 0 IRIN=1;" STARTS IN REGION 1, COULD BE 2 INITIAL WEIGHT = 1 SINCE NO VARIANCE REDUCTION USED 0 WTIN=1.0;" NRC VARIABLE FOR TRACKING THE HISTORY -NOT USED HERE 0 INRCIN=0;" 0 "NOW INITIATE THE SHOWER 10 TIMES 0 0 Õ DO I=1,10<OUTPUT I;(' START HISTORY', I4); 1 1 CALL SHOWER(IGIN, EIN, XIN, YIN, ZIN, UIN, VIN, WIN, IRIN, WTIN, INRCIN); 1 1 "NOTE THE OUTPUT IS DONE AT THE END OF EACH HISTORY IN SUBROUTINE AUSGAB"> 0 0 STOF; END; 0 0 0 0 0 0 SUBROUTINE AUSGAB(IARG); 0 0 . THIS ROUTINE WILL BE CALLED WITH IARG=3 WHENEVER A PARTICLE HAS 0 . BEEN DISCARDED BY THE USER IN HOWFAR 0 . 0 WE GET IT TO PRINT THE REQUIRED INFORMATION AT THAT POINT 0 0 0 Ö COMIN/STACK/; 0 0 IF(IARG.EQ.3)< ANGLE=ACOS(W(NP))*180./3.14159; ANGLE W.R.T. Z AXIS IN DEGREES 1 1 IF(IQ(NP).EQ.0)<EKINE=E(NP);> ELSE <EKINE=E(NP)-0.511;>*GET KINETIC ENERGY 1 OUTPUT EKINE, IQ(NP), ANGLE; (T21, F10, 3, T33, I10, T49, F10, 1);> 1 RETURN; END; 0 %E

Notes: i) For a sophistcated program there would be a great deal of I/O and statistical analysis in the main program. ii) AUSGAB is called under 21 well defined conditions which are specified by the value of IARG.

0	******	*****	*****			
0						
0	SUBROUTINE HOWFAR;					
0						
0		CTUEN & PARTICLE	AT (V.V.7) TH D	FRION TO AND GOING IN DISCOTION		
0	6	(ILLILL). THE PO	HI (ATTAL IN N	LE DIESTION, CAN THE PARTICLE CO		
0		A DISTANCE HETER	UTTUNIT CONCESSION	IC & DOUNDARY		
~	0	H DISTHICE USTER	TT MEDELY DETUDA			
0	 ∎	IF IES	II MERELI RETURN	TANCE TO DOUNDARY IN THE OURDENT		
0		IF NO, IT SETS USTEP=DISTANCE TO BOUNDARY IN THE CURRENT				
0	<u></u>	DIRECTION AND SETS IRNEW TO THE REGION NUMBER ON THE				
0	70 I	FAR SIDE	UP THE BOUNDART	(THIS CAN IN GENERAL BE MESSY!)		
0		THE HOLE ON TES	VINTE A UTOTODY			
0	5. 	THE USER CAN TER	MINALE A HISTURY	BY SETTING IDISC. O, HERE WE TERMINATE		
0		ALL HISTORIES WH	ICH ENTER REGION	A 3 OR ARE GUING BACKWARDS IN REGION 1		
0		7	ov 51			
0				1		
0		REGION 1	I REGION 2	I REGION 3		
0	8		1	1		
0		e- =======>	1	l e- or photon ====>		
0			1 22	1		
0	τ.	vacuum	I Ta	Ascnnw Ascnnw		
0						
0	******	*****	*****	***************		
0	COMIN/S	TACK, EPCONT, GEOM/	';			
0	8	COMMON STACK CON	TAINS X,Y,Z,U,V,	W AND IR		
0		COMMON EPCONT CO	NTAINS IRNEW, UST	TEP AND IDISC		
0		COMMON GEOM CONT	AINS ZBOUND			
0						
0	IF(IR(N	P).EQ.3) <idisc=1;< td=""><td>RETURN; "TERMINAT</td><td>TE THIS HISTORY: IT IS PAST THE PLATE"></td></idisc=1;<>	RETURN; "TERMINAT	TE THIS HISTORY: IT IS PAST THE PLATE">		
0						
0	ELSEIF(IR(NP).EQ.2)<"WE	ARE IN THE Ta PL	LATE - CHECK THE GEOMETRY		
1						
1	IF(W(NP).GT.0.0)<"GO	ING FORWARD -CON	NSIDER THIS FIRST SINCE IT IS MOST FREQUENT		
2		TVAL=(ZBOUND-Z(N	<pre>IP))/W(NP); *TVAL</pre>	L IS DISTANCE TO BOUNDARY IN THIS DIRECTION		
2		IF(TVAL.GT.USTEP) <return;"can ta<="" td=""><td>AKE CURRENTLY REQUESTED STEP*></td></return;"can>	AKE CURRENTLY REQUESTED STEP*>		
2		ELSE <ustep=tval;< td=""><td>IRNEW=3;RETURN;</td><td></td></ustep=tval;<>	IRNEW=3;RETURN;			
2		>"END OF W(NP)>0	CASE			
1						
1	ELS	EIF(W(NP).LT.0.0)	<"GOING BACK TOW	WARDS ORIGIN		
2	15 Mar 19 Carlos	TVAL=-Z(NP)/W(NF); DISTANCE TO	PLANE AT ORIGIN		
2		IF (TVAL.GT.USTEP) <return; can="" ta<="" td=""><td>AKE CURRENTLY REQUESTED STEP*></td></return;>	AKE CURRENTLY REQUESTED STEP*>		
2		ELSE <ustep=tval< td=""><td>IRNEW=1;RETURN:</td><td></td></ustep=tval<>	IRNEW=1;RETURN:			
2		>"ENT W(NP)<0 CA	SF			
1						
1	ELS	EIF(W(NP).EQ.0.0)	<"CANNOT HIT BOL	UNDARY "RETURN\$>		
-	>*F	ND OF REGION 2 CA	ASE			
ô						
ŏ	FLSETE(TR(NP), F0.1)<"TN	REGON WITH SOURC	CF		
1	IF	H(NP).GT.0.0)<"TH	TS MUST BE & SOL	URCE PARTICLE ON 7=0 BOUNDARY		
2	ISTEP=00.00:TRNEW=2:RETIRN:>					
1	FIG	ECTT MUST BE A	REFLECTED PARTIC	LE - DISCARD IT' IDISC=1:RETURN:>		
1	1.45	ND REGION 1 CASE		DIGONNO IT IDIGG-ITALIONATZ		
0	/ 6	WE VEDTOR I PHOE				
0	ENDINE		HOWEAR			
V NI	ENLY EN	In or SUPRUUTINE !		· · · · · · · · · · · · · · · · · · ·		
	nes: 1)	in general this	routine is the	e messy part - but it is conceptually		
SIL		requirements in	n the general c	case nave been completely specified by		
th	e in-line	comments.				

....

SLIDE 12

Parameters to be Set

AE,AP thresholds for secondary electron and brem production

ECUT,PCUT cutoffs for electron/positron and photon transport

ESTEPE electron maximum fractional energy loss per step

SMAX maximum length of electron step

Note: The last two parameters are not part of EGS but are essential at low energies as we see below. See Rogers 1984b.

SLIDE 14

Definitions of AE and AP

AE - for secondary or knock-on electrons if:

E _{sec} > AE	treat interactions discretely and follow secondaries
E _{sec} < AE	treat interactions as part of the continuous energy loss mechanism

AP - for bremsstrahlung generated photons if:

E _{brem} > AP	treat interaction discretely
E _{brem} < AP	treat as part of continuous energy loss mechanism

Notes: AE and AP are defined when calculating the cross-section data. One always has ECUT \ge AE and PCUT \ge AP.



Caption: Electron mean-free-paths in tissue between discrete interactions in which either knock-on electrons with total energies above AE keV or bremsstrahlung photons with energies above AP keV are created. The arrows denote the threshold energy for the production of knock-on electrons for that particular data set. The values were calculated by PEGS3. Notes:

i)AE is the total energy, including the rest mass

ii) lower values of AE mean more energy is lost via discrete events and hence the electron stopping power is smaller.

iii) The shape of the AE=521 keV curve makes one assumption used in EGS wrong since it doesn't decrease monotonically (see Rogers 1984b for a discussion - there appear to be no major consequences).



Caption: The electron energy spectrum as calculated by EGS after a beam of 20 MeV electrons has passed through an 0.25 cm slab of water. The data set used only allowed the creation of secondary electrons with kinetic energy greater than 1 MeV and hence there is a threshold 1 MeV below the peak corresponding to electrons which only lose energy in the slab via the continuous energy loss mechanism. A similar threshold occurs 100 keV below the peak. It corresponds to bremsstrahlung events creating 100 keV x-rays.

Note:

This spectrum is clearly not very realistic but in practice it often provides a sufficiently accurate model, see e.g. two slides on.

SLIDE 16



Caption: Electron spectra as in previous slide but for lower cutoff energies AE and AP and compared to the spectrum calculated with CYLTRAN (=ETRAN) which uses the Landau energy-loss straggling formalism. The EGS calculation for AE=512 keV, which explicitly includes all inelastic scatterings creating electrons greater than 1 keV, is in excellent agreement with the Landau approach to energy-loss straggling but takes considerably longer to calculate.

Note: The main concern when choosing values of AE and AP for a given value of ECUT is the effect on the energy-loss straggling.

SLIDE 18



Caption: Depth-dose curve for broad parallel beams of 20 MeV electrons incident normally on a thick slab of water. In all cases electron histories were terminated when the energy fell below 1 MeV kinetic energy(ECUT=1.5 MeV). Different data sets with AE = 0.521, 0.700, and 1.5 MeV total energy were used. These data sets have considerably different energy loss straggling, as shown in the previous two slides; nonetheless the effect on the depth-dose curve is very little.

However, there are situations in which the results are very dependent on the energy-loss straggling and hence to AE. For example, for 100 keV electrons incident on a foil which has a thickness equal to 70% of the electrons CSDA range, the calculated number of electrons which get through the foil changes from 8.2+-0.3% for AE=512 keV to 18.6+-0.4% for AE=521 keV which has much less energy straggling.



Caption: Variation as a function of ECUT in the calculated depth-dose curve for 100 keV electrons incident normally on a slab of water. As an electron's energy falls below ECUT the history is terminated and thus when the residual range at the energy ECUT becomes significant with respect to the depth bins being used, the depth-dose curve becomes compressed. In all cases AE = 10 keVkinetic energy, ESTEPE=4%, EGS3.

SLIDE 20



Caption: Variation in the depth-dose curve as a function of ECUT for a 20 MeV broad parallel beam of electrons incident normally on a slab of water. AE=521 keV (total energy) for all cases. There appears to be no statistically significant variation until ECUT is greater than 1.5 MeV.

Selection of ESTEPE

ESTEPE the maximum fractional energy loss per electron step. Not defined in EGS but can be set by adjusting the array TMXS. The default for low energy e⁻ in low 7 materials is about 20%. For completely accurate results, about 1% is needed for low 7 materials.

The following subroutine should be called from the users code after HATCH has been called in order to set TMXS for a specified value of ESTEPE.

•		
•	* FIXTHX *	
	t	- 2
SUBRO	JTINE FIXTHX(ESTEP, HEDIUH))	
	THIS PONITIME CHANGES THE STEP SIZE ALROBITIVAUSED IN FOS SO THAT	
•	THE STEP SIZE ARRAYS FOR THXS CORRESPOND TO AN ARBITRARY, BUT	
•	FIXED FRACTIONAL ENERGY LOSS ESTEP. ESTEP IS TYPICALLY 0.04.	
	THIS IS THE STEP SIZE ALGORITHN USED BY BERGER AND SELTZER IN ETRAN	1
	IT IS ONLY NECESSARY FOR LOW ENERGY ELECTRON PROBLEMS STRUCE	4
	THAN THIS 4% ENERGY LOSS FOR ELECTRONS WITH ENERGIES ABOVE A FEW NEV	
		1
	NOTE THAT THE STHXS-OVER-RIDE MACRO IS STILL IN FORCE IN EGS. IT	- 2
	HAT BE DESTRABLE TO KENUVE ITT	
•	THE ROUTINE CHANGES THE VALUES ONLY FOR THE MEDIUM 'MEDIUM'	
•	AND IT SHOULD PROBABLY BE USED FOR ALL MEDIA IN A PROBLEM.	1
	THE DOUTTHE WHAT HE CALLED AFTER MATCH MAD BEEN CALLED AND BEENDE	
	THE RUDITAL AUST DE CALLED AFTER MATCH MAS BEEN CALLED AND BEFORE	
	THE ALTOCATION 40 DEDUTT	
	THE ROUTINE IS INDEPENDENT OF WHAT UNITS ARE BEING USED, AS LONG	
•	AS THEY ARE CONSISTENT(E.O. CN, RL DR GH/CH442)	1
	NOTE THE PONITINE WAS NOTITEN FOR THE 3/8/28 UEDSTON OF FAST.	1
	IN PARTICULAR, THIS MEANS THE SET INTERVAL MACRO HAS A DUNKY THIRD	
•	ARGUMENT AND THE MAPPING FEATURE HAS NOT BEEN IMPLEMENTED.	
•		1
	VO1 DEC 10,1981 DAVE ROGERS WRCC	1
•SET	UP SOME VARIABLES FOR FIRST PASS THROUGH LOOP"	
EI = '	EXP((1,-EKEO(MEDIUM))/EKE1(MEDIUM))/"EMERGY OF FIRST TABLE ENTRY"	
LEILA	IF THIS IS EQUIVALENT TO ASETINTERVAL EIL, EKE, DUMHY/BUT AVOIDS ROUNDOFF	
SITES	UATE EDEDX USING EDEDX(EIL)1*PICK UP THE ELECTRON STOPPPING AT EI* Calculate The Step Required to Cause an Estep Reduction in Emergy* Tepfei/EdeDXi	
-	ATER ENERGIER ARE IN A FIVER PATTO - CALC LOS OF THE PATTO	
ERATI	Q=-1./EKE1(HEDIUH))	
NEKE=	MEKE(MEDIUM) I'NUMBER OF ELEMENTS IN STORAGE ARRAY"	
DO I=	1+NEKE-1<	
E	IP1=EXP((FLOAT(I+1)-EKEO(WEDIUM))/EKE1(WEDIUM)))'ENERGY AT I+1"	
1	EVALUATE EDEDX USING EDEDX(EIP1L)ISIP1=ESTEP#EIP1/EDEDXI	
	HALL CALLE THERE CONSTANT	10
	NUM BULYE INEBE ENVILLUMB	
	SI = THXS1 # EIL + THXS0	
	SIP1 = THXS1 # EIP1L + THXS0	
÷	FOR THXSO(I, MEDIUM) AND THXS1(I, MEDIUM)	
:	FOR THISO(I,MEDIUH) AND THISI(I,MEDIUH) HISI(I,MEDIUH)=(SI-SIPI)/ERATIO:	
	FOR TRXSO(I;HEBIUH) AND TRXSI(I;HEDIUH) HXSI(I;HEBIUH)=(SI-SIPi)/ERATIO; HXSO(I;HEDIUH)=SI-THXSI(I;HEDIUH)#EIL)	
	FOR TRXSO(I;HEDIUH) AND TRXSI(I;HEDIUH) NXSI(I;HEDIUH)=(SI=SIP1)/ERATIO NXSO(I;HEDIUH)=SI-TRXSI(I;HEDIUH)#EIL) TRANSFER VALUES FOR HEXT LOOP*	
	FOR TRXSO(I,HEDIUH) AND TRXSI(I,HEDIUH) NXSI(I,HEDIUH)=(SI-SIPI)/ERATIO NXSO(I,HEDIUH)=SI-TRXSI(I,HEDIUH)BEIL) TRANSFER VALUES FOR WEXT LOOP* IL-EIPILISI=SIPI	
T T	FOR TRXSO(I=HEBIUH) AND TRXSI(I=HEBIUH) NXSI(I=HEBIUH)=(SI=SIPI)=ERATIO# NXSO(I=HEBIUH)=SIT=TRXSI(I=HEBIUH)#EIL) TRANSFER VALUES FOR HEXT LOOP* IL=ETPILISI=SIPI	





Caption: Transmission and reflection factors for a 2 MeV beam of electrons incident normally on a 3 mm thick slab of silicon as a function of ESTEPE. The default EGS case is shown as 18%. The default calculations take 0.08 s/history whereas the 1% calculations take 0.55 s/history and the 0.1% calculations take 4.8 s/history. Notes:

i) ESTEPE clearly has a dramatic effect on the results and the timing.

ii) ETRAN uses a comparable algorithm and energy loss per scattering step of around 1% or less.

iii) The basic cause of this ESTEPE dependence appears to be related to the difference between the curved pathlength and straight pathlength taken by the electron in the simulation. The approximate correction technique used in EGS appears to be wrong. By going to suffciently small steps the problem is avoided since there is no difference between the true curved pathlength and the straightline pathlength. ETRAN and other Monte Carlo codes make no correction for this difference and so they must use very short steps too. See Rogers 1984b for more discussion.





Caption: Absorbed dose to water vs depth as a function of the maximum continuous energy loss per step for 100 keV electrons incident on a water slab. The step-size has a 50% effect on the peak value in the depth-dose curve. As ESTEPE goes below about 1% the multiple scattering formalism is turned off more and more until it is completely turned off for ESTEPE=0.1%. Note:

The problem of turning off the multiple scattering if too small a step-size is used makes life difficult in high precison work since there is only a narrow range of ESTEPE values which give the "correct" result. See Rogers 1984b for a discussion of this problem.



Caption: Dose delivered to a 2mm diameter, 20cm long tube of air by a pencil beam of 1 MeV electrons incident on the axis as a function of SMAX, the maximum length of each electron step. The values are normalized to the dose for SMAX=2mm. The value calculated with CYLTRAN (=ETRAN) is shown on the same curve although there is no corresponding parameter. Note:

This is a dramatic demonstration of the "thin slice effect" discussed by Bielajew et al,1984. It is related to the difference between the curved pathlength and the straight line pathlength and is only important whenever one or two dimensions of the volume of interest are comparable to the electron step-size, e.g. very thin slices in a phantom or an ion chamber cavity.

SLIDE 24

Considerations in Parameter Selection

AE,AP -energy loss straggling, lower limit on ECUT,PCUT

ECUT, PCUT-residual range of particles

ESTEPE -pathlength correction, multiple scattering

SMAX -to avoid thin slice effect

SLIDE 26

Variance Reduction Techniques

i) exponential transformation of photon pathlength

- ii) forced photon interactions
- iii) range rejection of electrons
- iv) use of stored pre-computed results

v) optimize ECUT

Note: For certain cases, a smaller ECUT can increase the efficency of the calculation (e.g. ion chamber response -see Bielajew et al,1984).

i)Exponential Transformation of Photon Pathlength

use:

$$mfp = -B.lnR_i$$

WT' = WT.B.e^{-mfp.C.cosZ}

with

$$B = 1./(1.-C.cosZ)$$

where C is an input variable, mfp is the number of photon mean free paths, R is a random number from 0 to 1, and $\cos Z$ is the direction cosine w.r.t. the Z axis.

C **∠**-1 pathlength shortening -Study Buildup

0 < C < 1 pathlength stretching -shielding

SLIDE 28

Calculational Efficiency vs C for 7-MeV Photons on a 30cm slab of Water

C	Histories	Relative Efficiency on Calculated Dose			
	103	0-0.25cm	6-7cm	10-30cm	
0	100	11	1.4	0.16	
-1	70	11	1.4	0.04	
-3	55	7.8	1.2	0.25	
-6	50	4.0	0.5	2.3	

Notes:

i) Calculational efficiency is taken here as the square of the uncertainty on the calculated doses for a series of calculations using the same CPU time.

ii) This is a very common technique in neutron monte carlo work.

iii) $C \leq -1$ increases the number of photon interactions near the surface but reduces their weight. For a depth-dose curve we score the weightxenergy deposited. The effect of scoring more electrons, each with a reduced weight, is to reduce the statistical variation although we also increase the computing time per history. It is not always clear how much improvement there will be.

iv) Its effectiveness is very problem dependent. Here the efficiency increases by a factor of 3 near the surface as C increases but the efficiency at depth worsens since we are decreasing the number of interactions there. v) 0 < C < 1 is very useful in deep shielding problems.

ii) Force Photon Interactions

For a photon with a given energy, location and direction, find X, the number of mean free paths it must traverse before leaving the object of interest. Then use:

$$mfp = -ln(1-R_i(1-e^{-X}))$$

WT' = WT . (1-e^{-X})

where R_i is a random number from 0 to 1 and mfp is the number of mean free paths to traverse before interaction (note mfp X).

Note:

i) In general the only difficulty is finding X. However we have developed a general purpose macro which can be used in any EGS geometry to determine X and then mfp and WT'. This works in the general case because it calls the users routine HOWFAR to determine certain characteristics of the geometry (see next page)

ii) The improvements in calculational efficiency are very problem dependent. Define efficiency as the total computing time required to achieve a certain statistical uncertainty on the result of interest. a)In calculating the response to ⁶⁰Co of an ion chamber in which

6% of photons would normally interact, forcing improves

efficiency by 60% (see Bielajew et al,1984). b)In calculating the dose from Co in an 0.001cm slice of tissue in which 6x10 of the photons interact, the efficiency improves by a factor of 2600 (see Rogers and Bielajew, 1984). c)In calculating the dose from ⁶⁰Co interacting in 100 cm of air

the efficiency improves by a factor of 7.

SLIDE 30

iii) Range Rejection of Electrons

Terminate any electron which is greater than its CSDA range from:

a)the region of interest (e.g. an ion chambers cavity)

OL

b) any region boundary (specified by DNEAR).

Notes:

i) For ion chamber calculations, method a) improves the calculational efficiency by a factor of 4 when a good estimate of the CSDA residual range is used.

ii) Technique b) can be crudely implemented in EGS in a general fashion for low electrons. Since the electron stopping power dE/dx is initially energy monotonically decreasing with energy, then the range is always less than 1/(dE/dx). Thus one can safely terminate the electron history whenever 1/(dE/dx) is less than DNEAR (the distance to the nearest boundary as returned by HOWFAR).

iii) Implementing these techniques ignores the possibility of bremsstrahlung emmission by the terminated electron if it were allowed to slow down.

"THE PHOTON IS FORCED TO INTERACT BEFORE HITTING REGION 1" "INSERT THE MACRO RIGHT AFTER THE \$RANDOMSET RNN035; STATEMENT IN PHOTON" ***** WARNING! DELETE ALL COMMENTS INSIDE THE MACRO BEFORE USING. ***** %'\$SELECT-MEAN-FREE-PATHS;'='; "FIRST STORE ANY VARIABLE THAT CAN BE CHANGED BY SUBROUTINE HOWFAR." DUMU=USTEP; DUMX=X(NP);DUMY=Y(NP);DUMZ=Z(NP); IRODUM=IROLD; IRNDUM=IRNEW; IRDUM=IR(NP); MEDDUM=MEDIUM; IDUM=IDISC; PATHL=0.0; "ZERO THE MEAN FREE PATH COUNTER" MEDIMP=0; "ASSUME THE INITIAL MEDIUM IS VACUUM" "NOW LOOP THROUGH ALL REGIONS ALONG THE PHOTON'S LINE OF FLIGHT" LOOP< USTEP=VACDST; "ASSUME A LARGE DISTANCE TO THE NEXT REGION; HOWFAR WILL TRUNCATE" IROLD=IR(NP);MEDIUM=MED(IROLD); STORE THE REGION & MEDIUM NUMBERS THAT MAY. "BE CHANGED BY HOWFAR" IF (MEDITMP, NE, MEDIUM) <"THE MACROSCOPIC CROSS SECTION CHANGES ONLY IF THE" "MEDIUM CHANGES" MEDTMP=MEDIUM; IF (MEDIMP.NE.0) <"TRANSPORT THROUGH VACUUM DOES NOT INCREMENT THE NUMBER" "OF MEAN FREE PATHS TRAVERSED-DELTAP IS GAMMA MEAN FREE PATH IN THIS MEDIUM" \$SET INTERVAL GLE, GE, GEM; \$EVALUATE DELTAP USING GMFP(GLE);> CALL HOWFAR; "SET USTEP AND SWITCH IRL, MEDIUM TO THE NEXT REGION" IF (MEDTMP.NE.O)PATHL=PATHL+USTEP/DELTAP; "INCREMENT THE # OF MEAN FREE PATHS" IF(IRNEW.EQ.1) EXIT; "EXIT THE LOOP IF THE PARTICLE IS LEAVING THE GEOMETRY" *DO A FAKE TRANSPORT TO GET THE CORRECT COORDINATES FOR THE NEXT PASS THROUGH* "THE LOOP" IR(NP)=IRNEW; X(NP)=X(NP)+USTEP*U(NP); Y(NP)=Y(NP)+USTEP*V(NP); Z(NP) = Z(NP) + USTEP * U(NP);> "END OF THE PATHLENGTH SUMMATION LOOP" "RESTORE THE VARIABLES THAT MAY HAVE BEEN ALTERED BY HOWFAR" USTEP=DUMU; X(NP) = DUMX; Y(NP) = DUMY; Z(NP) = DUMZ; IROLD=IRODUM; IRNEW=IRNDUM; IR(NP)=IRDUM; MEDIUM=MEDDUM; IDISC=IDUM; "CALCULATE THE PROBABILITY THAT THE PHOTON INTERACTS" GWAIT=1.-EXP(-PATHL); "ADJUST THE PHOTON'S WEIGHT SO THAT PROBABILITY IS CONSERVED" WT(NP)=WT(NP)*GWAIT; "RANDOMLY SELECT THE NUMBER OF MEAN FREE PATHS UNTIL THE INTERACTION THAT" "IS GUARANTEED TO BE IN THE GEOMETRY" DPMFP=-ALOG(1,-RNN035*GWAIT); "THE # OF MEAN FREE PATHS CORRECTLY SAMPLED" "RNN035 IS A RANDOM NUMBER BETWEEN 0 AND 1" " "END OF THE FORCING-INTERACTIONS MACRO" \$

MACRO WHICH FORCES A PHOTON INTERACTION TO OCCUR WITHIN THE VOLUME *OF INTEREST WITH THE BOUNDARY BEING DEFINED AS INSIDE REGION 1,1.E.*

iv) Fold Pre-computed Results



Notes:

In many calculatons we want the dose at a depth in a phantom due to electrons and photons generated in a complex geometry. Only a few particles get to the phantom so the dose calculated by tracking them in the phantom is very inaccurate. By just scoring the particle fluence as it reaches the phantom surface, and later folding it with pre-computed depth-dose curves, one makes an large gain in computing efficiency; the statistical uncertainty in the dose becoming comparable to the statistical uncertainty in the fluence.

The method introduces several approximations because it uses pre-computed conversion factors $K_{E}(d)$ (e.g. from Rogers,1984a) which are for broad parallel beams of particles incident normally on a tissue phantom. As we have implemented this procedure, we have not considered electrons below 100 keV and so we underestimate the dose in the first 12 mg.cm⁻².

SLIDE 32



Caption: Comparison of various methods of computing the central axis dose in a tissue phantom due to electrons generated by a point source ⁶⁰Co beam hitting the phantom at SSD = 200 cm (beam diameter=35 cm at SSD=80cm). ECUT=611 keV total energy in all cases. The curves labelled "Full Simulation" tracked the electrons and photons through the air and into the phantom. In the lower of these, the electrons were artificially adjusted to have normal incidence at the phantom surface, thus reducing the surface dose, much of which is due to highly scattered low energy electrons. The curves marked "Folded" were done simulating the electron transport in the air and scoring either the planar fluence or the true particle fluence (which includes a 1/cosZ weighting factor) at the phantom surface.

Notes:

The curve we usually use is that folded with the planar fluence and it is, as expected, in excellent agreement with the normally incident full simulation. The result obtained by folding with the true fluence is more accurate near the surface since there it more properly accounts for the angular incidence; however it does not take into account the contraction of the depth-dose curves due to the angular incidence and hence substantially overestimates the dose at depth.

The statistical uncertainties are smaller for the folded calculations than for the full simulation and thus the ratio of calculational efficiencies is even greater than shown by the ratio of CPU times.





Caption: Same physical situation as in the previous slide but here we look at results of the full simulation as we change ECUT. The inclusion of electrons with kinetic energies between 10 and 100 keV increases the dose for depths down to 10mg.cm⁻², making less difference when normal incidence is forced at the phantom surface. Note that only 100 keV electrons generated within 13 cm of the phantom can reach it.



SLIDE 34

INCIDENT BEAM RADIUS

Caption: The percentage values on the right are the decrease at that photon energy between the peak dose in a broad parallel beam and that in a beam of radius 0.5 cm. This shows that using coefficients for broad beams can introduce overestimates of up to a factor of 2 when the beam is actually very narrow.

Summary of Variance Reduction Techniques

 i) Exponential transformation of photon pathlength -factor of 2 or 3 in the buildup region
 ii) Force photon interactions -2,7 or 2600 times more efficient

iii) Range rejection of Electrons - factor of 4 in a cavity chamber cal'n.

iv) Fold pre-computed results - more than 10 times as efficient but introduces approximations.





This is the geometry we have modeled to study electron contamination from a 60 Co therapy source. We have implemented most of the variance reduction techniques discussed above and added a few further tricks. We start with the encapsulated Co source. By compressing into one 32 bit integer all the information concerning each particle leaving the front face of the capsule, we store, the results of a 24 hour simulation of the source capsule and reuse the 2×10^6 electron and photon histories as an input to the second stage of the calculation which simulates the therapy head. Range rejection is done in all the filters and collimators. All primary photons leaving the source can be optionally forced to interact before leaving the outer filter. This is used as a break point. The particles leaving the head are reused as inputs for the simulation of the transport to the scoring surfaces at different SSDs. Once again primary photons can be forced in this last stage through the air. The fluence (planar or true) is determined at each SSD as a function of radius and depth-dose curves are determined using pre-computed depth dose curves.

Benchmark Comparisons

A major advantage of using a standard code is that benchmark comparisons which have been done for it produce confidence in its ability to give accurate results for your problem. Unfortunately they don't guarantee that you have used it accurately.

Note:

In the following slides we present a series of benchmark comparisons of EGS against experimental data or other calculations. They are drawn from our work at NRCC and involve low energy applications in which electron transport plays an important role. There are many other benchmark examples for higher energies. We would appreciate having our attention drawn to other comparisons.



Caption: Measured and calculated response of a 3"x3" NaI detector with a 1.18g.cm⁻² beta absorber on its face to 3.07×10^{-661} -keV photons from an isotropic source 10 cm away in a lead box. The open circles represent the calculations with no absorber. The inclusion of the absorber accounts for the filling in of the valley. There are no free parameters in the comparison. The calculations did not take into account the lead box and thus did not produce a backscatter peak. The low energy peak is from an associated X-ray peak in the source which was not included in the calculations (taken from Rogers, 1982). Agreement within 2% has also been obtained between the measured and calculated efficiency of a 5"x4" NaI to 6.13 MeV photons (Mach and Rogers 1983).

SLIDE 38



Caption: A comparison of the measured absorbed dose vs depth in a $16\times16\times30$ cm water phantom and that calculated with EGS for a nearly monoenergetic 7-MeV photon beam and the associated electron contamination. The ion chamber calibration factor was assumed to be depth independent. The comparison at 5 cm is absolute and there is agreement within 1+-3%.

The details of the comparison are complex but basically confirm the fluence to absorbed dose factors calculated with EGS for 7-MeV photons. (Taken from Mach and Rogers, 1984).



Caption: A comparison of various calculations of the depth-dose curve for broad parallel beams of 20 MeV electrons incident on a water phantom. The differences between the ETRAN and EGS results persist at other energies in water (but not, e.g. in copper) and the good agreement with Nahum's results also persists at other energies. (Figure from Rogers, 1984a, other results from Berger and Seltzer 1969 and Nahum, 1975).





Caption: Comparison of calculated results to experimental results presented in NCRP Report 51 for the angular distribution of dose from 8,3 and 2 MeV electrons incident on 5.79 g.cm⁻² of W. EGS is known to overestimate the bremsstrahlung cross-section for low-energy electrons because it ignores the Elwert correction factor. The agreement here for 8 MeV and at higher energies as well is very satisfactory. The dip at 90° is because the calculations are for a semi-infinite target. (Taken from Ewart and Rogers 1983).

SLIDE 42



Caption: Comparison of a measured contaminant free buildup curve for a zero area ^{6U}Co beam incident normally on a phantom (from Higgins et al,1984) with the calculated depth-dose curve for a broad parallel beam of ^{6U}Co incident on a water phantom (radiation scattered in the source is not included in the calculations, from Rogers and Bielajew,1984).



Caption: The fraction of 1 MeV electrons transmitted by various thicknesses of aluminium as calculated by EGS3 and EGS4 (with AE=521 keV,ECUT=551 keV) and ETRAN (Seltzer and Berger, 1974). The slight difference between EGS and ETRAN for calculated transmission factors persists in other cases as well. The experimental data is somewhat scattered but with a slight preference for the ETRAN results.

SLIDE 44



Caption: A comparison of the measureed and calculated increase in response measured in a cavity inside a PMMA phantom vs the total amount of irradiation by electrons. Because the phantom is an insulator, the incident electrons can remain in the phantom after they lose their energy. This sets up electric fields that can focus the electrons into the cavity producing an extra dose there. The EGS system has been modified to allow for transport in an electric field. In this case the electron beam energy is 5.7 MeV, the cavity is 0.35 cm in radius at a depth of 1.5 cm in the phantom (from Rawlinson et al,1984).



Caption: Calculated response to a 60 Co beam incident on the flat face of an 0.5 g.cm⁻² carbon walled pancake ion chamber, 1 cm radius, as a function of chamber depth. The calculated values agree within 1% with the values predicted by Bragg-Gray cavity theory (from Rogers et al, 1984). AE=ECUT=521 keV total energy, ESTEPE=1%.

SLIDE 46



Caption: Comparison of dose deposition at an aluminium-water interface irradiated by 60 Co as calculated by EGS and CYLTRAN (ETRAN). These type of interface calculations are very sensitive to ESTEPE which was 1% in this case.

-47-

Bibliography

- M.J.Berger and S.M.Seltzer, 1969, "Calculation of Energy and Charge Deposition and of the Electron Flux in a Water Phantom Bombarded with 20 MeV Electrons", Annals of the New York Acad.Sci 161,8.
- A.F.Bielajew, D.W.O.Rogers and A.E.Nahum,1984, "Monte Carlo Simulations of Ion Chamber Response to ⁶⁰Co" in preparation
- G.M. Ewart and D.W.O.Rogers, 1982, "Calculated thick target bremsstrahlung angular distributions and shielding calculations", Unpublished Report PXNR-2640, N.R.C. Ottawa
- R.L.Ford and W.R.Nelson, 1978, "The EGS Code System", Stanford Linear Accelerator Center Report No.210, Stanford, California
- P.D.Higgins, C.H.Sibata, R.P.Paliwal, 1984, "Determination of Contamination- free buildup for ⁶⁰Co", in press P.M.B.
- H.Mach and D.W.O.Rogers, 1983, "An absolutely calibrated source of 6.13 MeV gamma-rays", IEEE Trans.N.S. 30,1514-1517.
- H.Mach and D.W.O.Rogers, 1984, "A measurement of absorbed dose to water per unit incident 7-MeV photon fluence", in press P.M.B.
- A.E.Nahum, 1975, "Calculations of electron flux spectra in water irradiated with megavoltage electron and photon beams", PhD Thesis, University of Edinburgh
- W.R.Nelson, A.Hirayama and D.W.O.Rogers, 1984, "The EGS 4 Code System" SLAC Report No.265, in preparation.
- J.A.Rawlinson, A.F.Bielajew, D.M.Galbraith and P.Munro, 1984, "Theoretical and experimental investigation of dose enhancement due to charge storage in electron-irradiated phantoms", in press, Medical Physics.
- D.W.O.Rogers, 1982, "More realistic Monte Carlo calculations of photon detector response functions", Nucl.Instr.and Meth. 199,531-548.
- D.W.O.Rogers, 1984a, "Fluence to dose equivalent conversion factors calculated with EGS3 for electrons from 100 keV to 20 GeV and photons from 11 keV to 20 GeV", Health Physics 46, 891-914.
- D.W.O.Rogers, 1984b, "Low energy electron transport with EGS", in press Nucl.Instr.and Meth.

- D.W.O.Rogers and A.F.Bielajew, 1984, "Calculated buildup curves for photons with energies up to ⁶⁰Co", in preparation
- D.W.O.Rogers and G.M.Ewart, 1984, "Preliminary report on a project to study beam contamination from ⁶⁰Co head", unpublished report PXNR 2682, NRC, Ottawa
- D.W.O.Rogers, A.F.Bielajew and A.F.Nahum, 1984, "Ion chamber response and A_{wall} correction factors in a ⁶⁰Co beam by Monte Carlo simulation", in preparation.
- S.M.Seltzer and M.J.Berger, 1974, "Transmission and reflection of electrons by foils", Nucl.Instr.and Meth. <u>119</u>,157.