

Monte Carlo simulation of electron-photon transport: from particle physics to cancer radiotherapy

D. W. O. Rogers
Physics Dept,
Carleton University
Ottawa



<http://www.physics.carleton.ca/~drogers>
Cameron Lecture, U Wisconsin, Sept 13, 2004

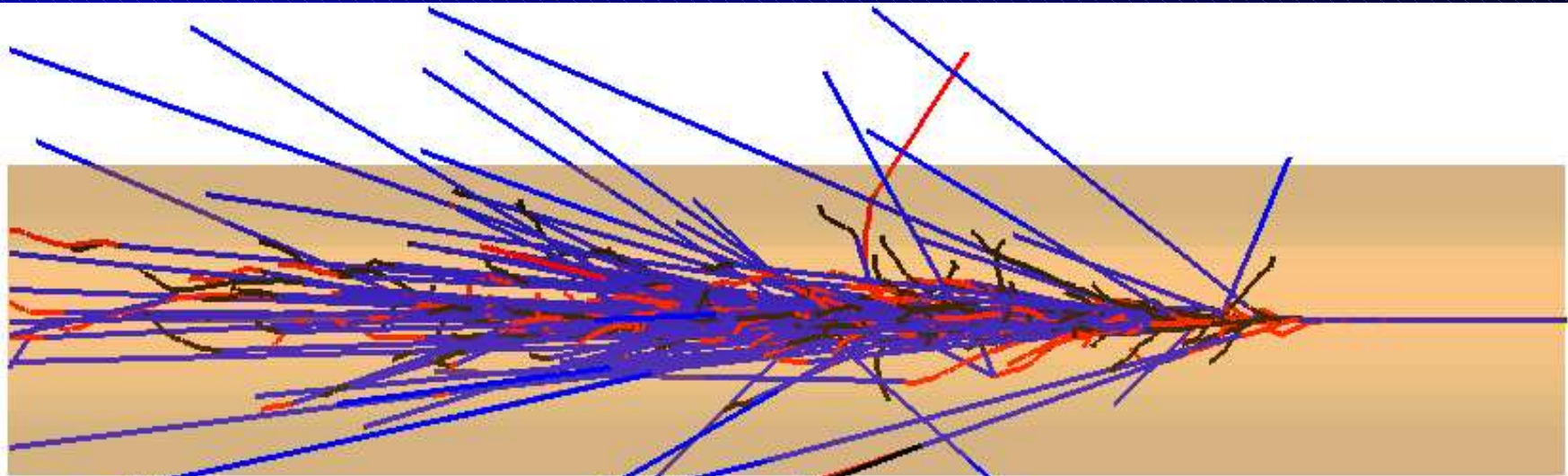
Overview

- a 10-fold increase in the efficiency of the **BEAM code** (with Iwan Kawrakow and Blake Walters)
- **brachydose**- an efficient code for Monte Carlo dose calculations in brachytherapy (with Gultekin Yegin)
 - **inter-seed effects** in ^{125}I prostate treatments
- a **correlated sampling code** to increase efficiency of dosimeter calns with EGSnrc (with Lesley Buckley and Iwan Kawrakow)
 - OSL and electrode correction examples

Monte Carlo transport

- simulate paths of many particles
 - use random numbers
 - known probability distributions
 - from physics of interactions
- keep track of physical quantities
 - learn average properties
 - stochastic distributions of events

EGS: Electron Gamma Shower



Photons

Electrons

positrons

10 GeV photon from
right on 10 cm lead
cylinder

EGS3 Ford and Nelson, SLAC 1978

EGS4 Nelson et al, SLAC, NRC 1985

BEAM code

- general purpose code to simulate **radiotherapy beams**
 - accelerators -electrons & photons
 - ^{60}Co units
 - x-ray units
- Part of the **OMEGA project** with **Rock Mackie's** group in Madison
 - many grad students, RAs and TOs involved

BEAM developers

Dave Rogers

Blake Walters

Charlie Ma

Bruce Faddegon

Jiansu Wei

George Ding

Geoff Zhang

Joanne Treurniet

Michel Proulx

Daryoush Sheikh-Bagheri

Iwan Kawrakow

EGS4: Ralph Nelson and Alex Bielajew

EGSnrc: Iwan Kawrakow

vacuum
exit

scanning
magnet

monitor
chamber

jaws

Therac 20
20 MeV electrons

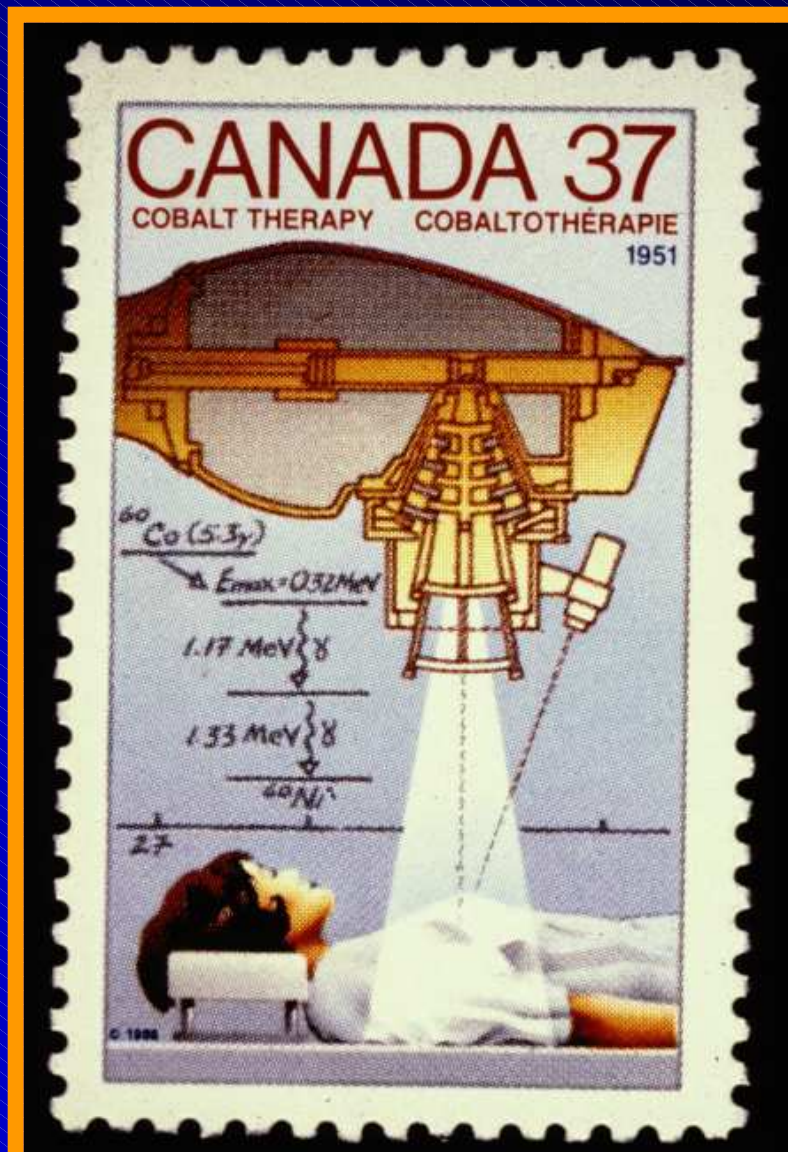
applicator

patient

electrons blue
photons yellow

^{60}Co therapy unit

Issued
June 17,
1988



Thanks to
Jerry Battista

What is efficiency?

$$\epsilon = \frac{1}{\sigma^2 T}$$

T : computing time

σ^2 : variance on quantity of interest

- sum of uncertainty²

- **fluence** in 1x1cm² regions in beam

- **dose** on central axis or profile

Problems to overcome

-in photon accelerators, majority of time is spent **following electrons**

-most photons are absorbed in the **primary collimator**

Uniform Brem Splitting (UBS)

-when an electron undergoes a radiative event, create n_{split} photons with weight $1/n_{\text{split}}$

-overcomes most time being for electrons

-particles have same weight

EGSnrc has an efficient algorithm

Russian Roulette

Still creating a large number of **electrons** in collimators, jaws etc

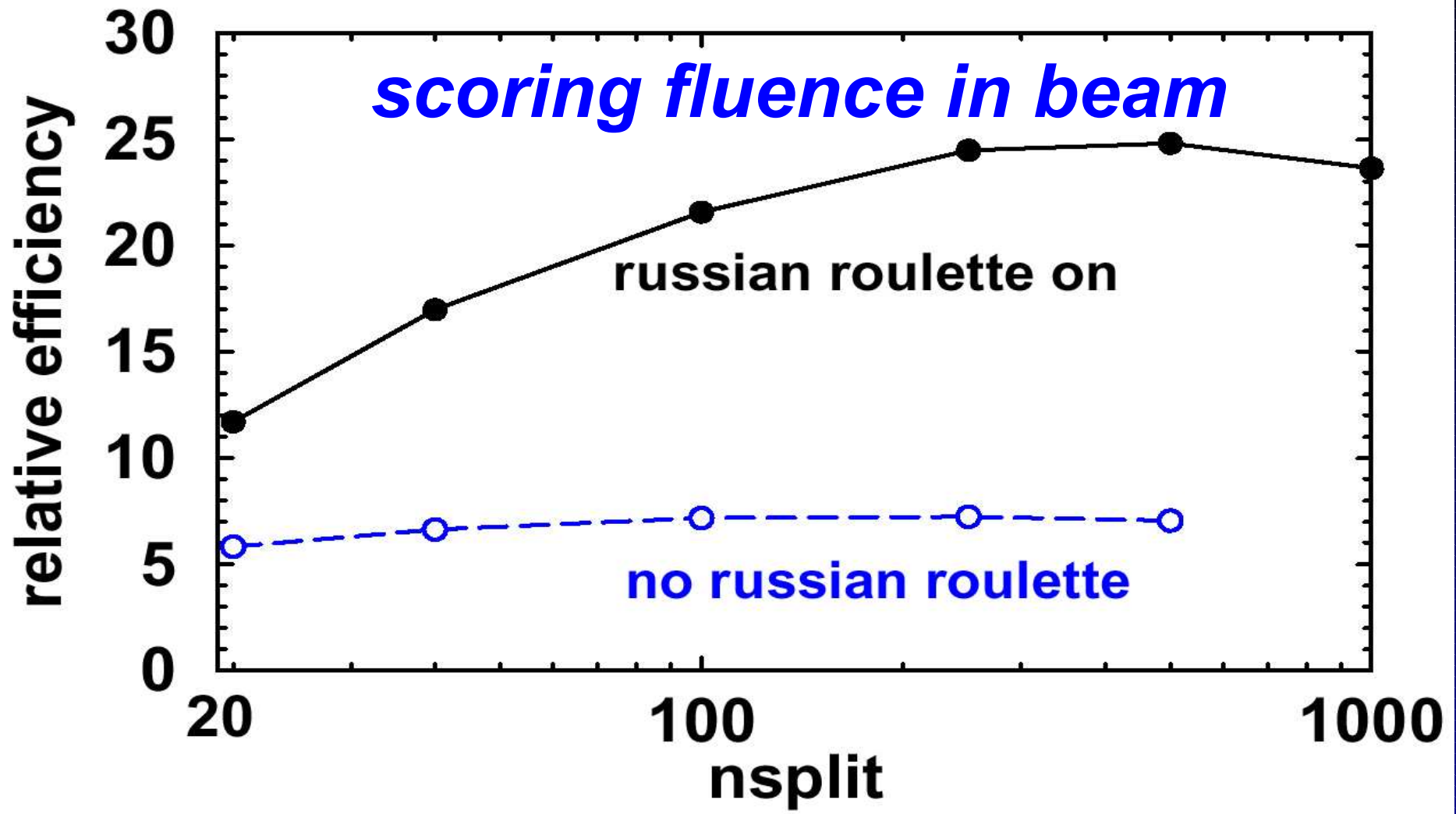
-play **Russian Roulette** on **secondary electrons**
(weight of e^- is 1)

-**split n_{split}** times in further radiative events

=> **photons weight still $1/n_{split}$**

=> not many electrons in **phase space**

Uniform Brem Splitting



Selective Brem Splitting (SBS)

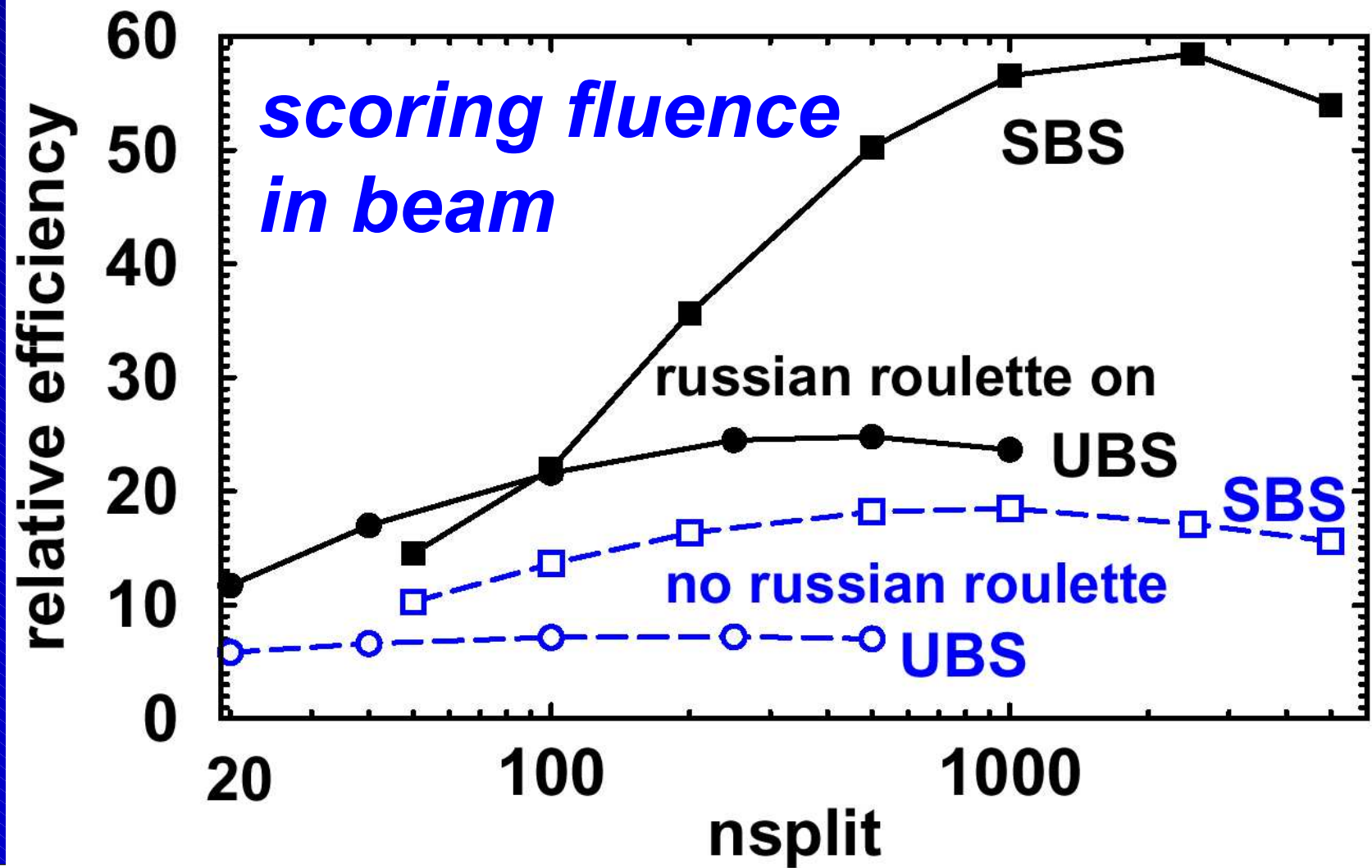
Daryoush Sheikh-Bagheri

-split photons more often **if likely to be in the beam** (calculated probability)

-`fat' photons a problem

=> **minimum split** about 10% of max

Selective Brem Splitting (SBS)



SBS problems

- large **variation in weights**
'fatter' photons still affect efficiency
- wasting lots of time on electrons which **cannot get to the phase-space file**
- with Russian roulette on, the **electron efficiency** is poor

Directional Brem Splitting (DBS)

-goal: **all particles in field** when reach phase space have **same weight**

Procedure

- i) brem from **all fat** electrons split **nsplit** times
- ii) if photon **aimed at field** of interest, **keep it**, otherwise Russian roulette it:
if it survives, weight is 1 (i.e. fat)
- iii) if using **only leading term** of Koch-Motz angular dist'n for brem: **do_smart_brems** and similar tricks for other interactions

DBS (cont)

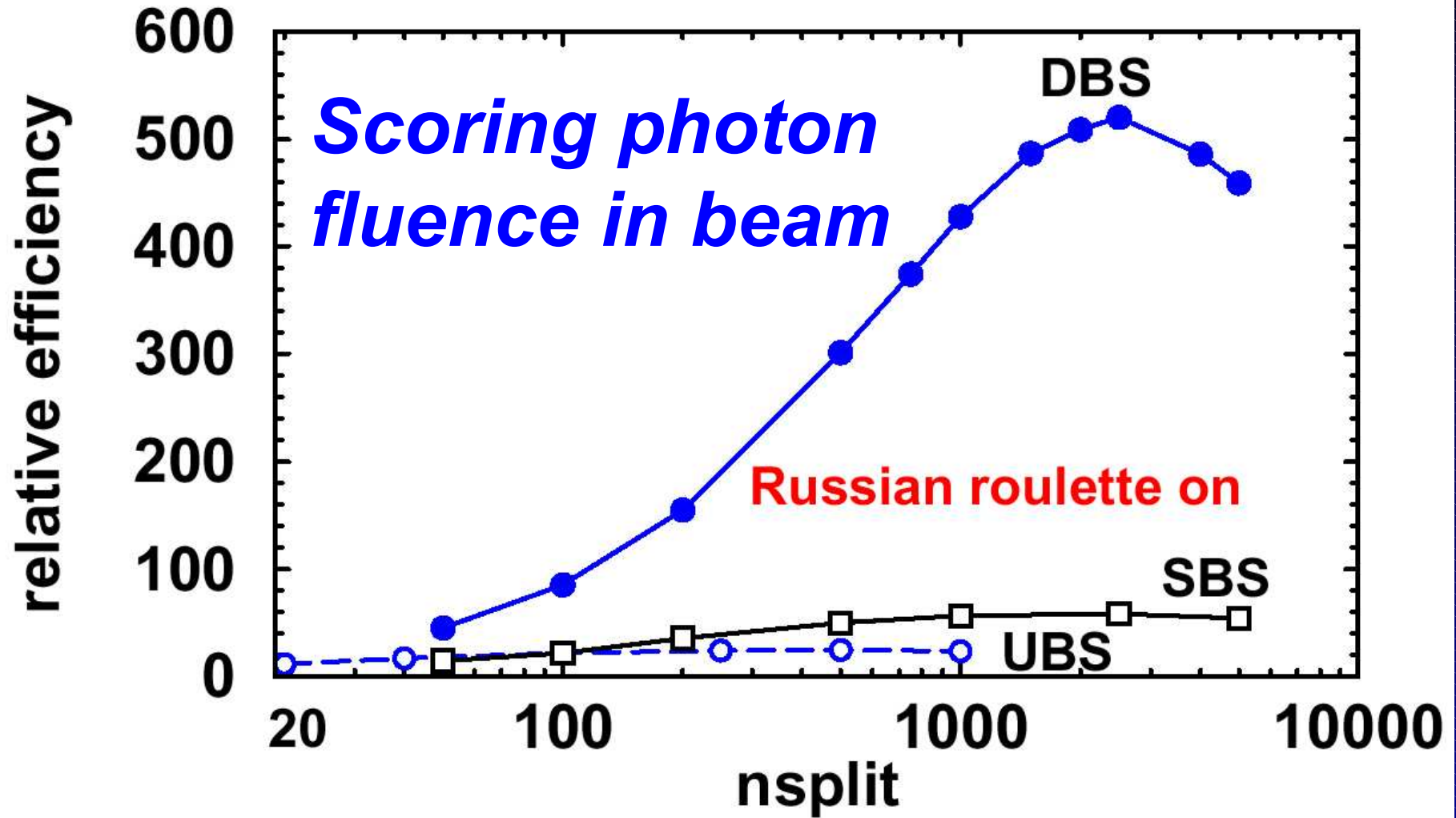
photons

- reaching field have weight $1/n_{split}$
- outside field are fat

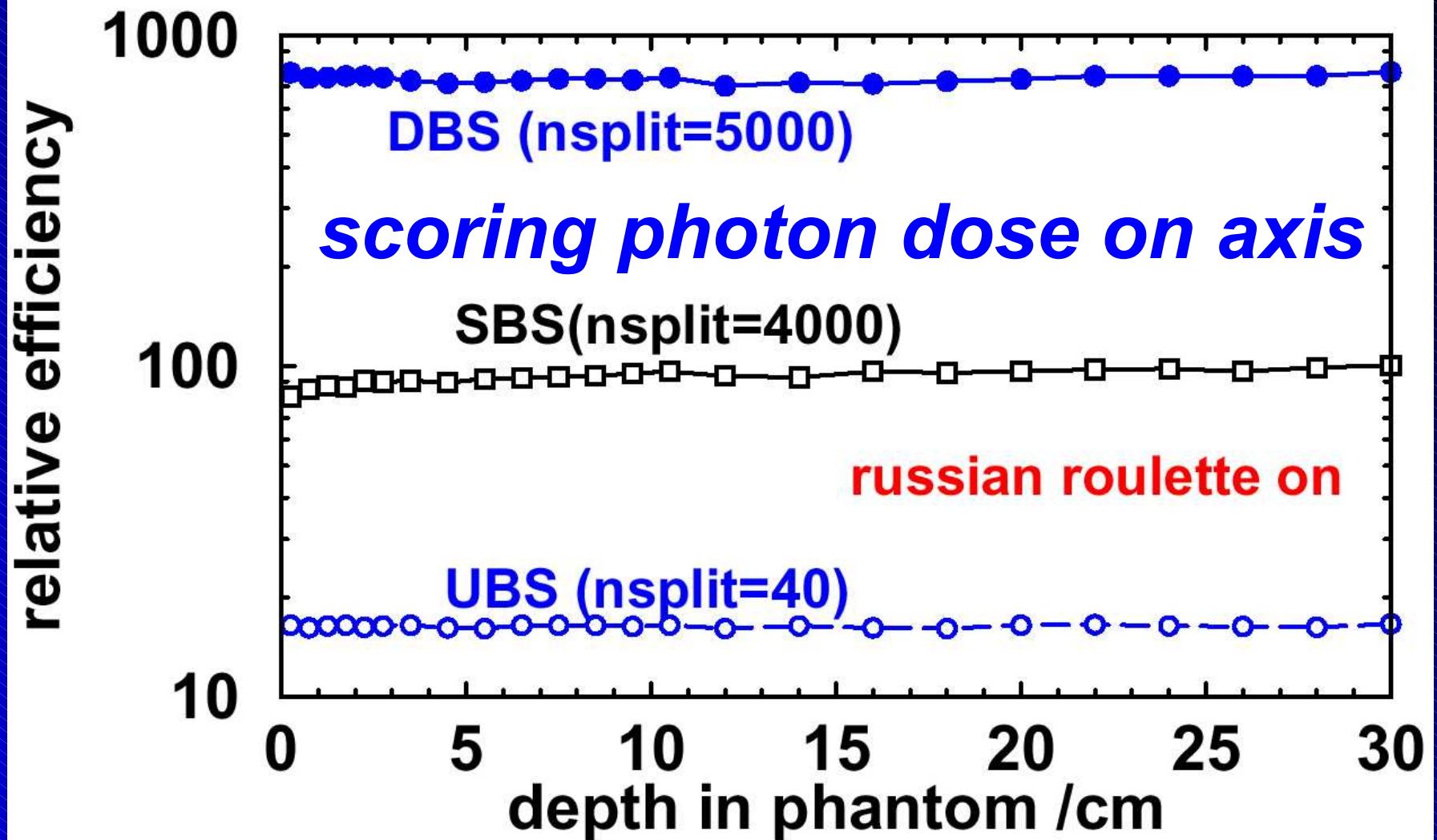
electrons in the field

- usually fat
- a few have weight $1/n_{split}$ from interactions in the air

Directional Brem Splitting



Directional Brem Splitting



Electron problem

-efficiency gain for electrons is only 2

Basis of the solution

-electrons are, almost entirely, from flattening filter and below

-major gains are from treatment of electrons in primary collimator

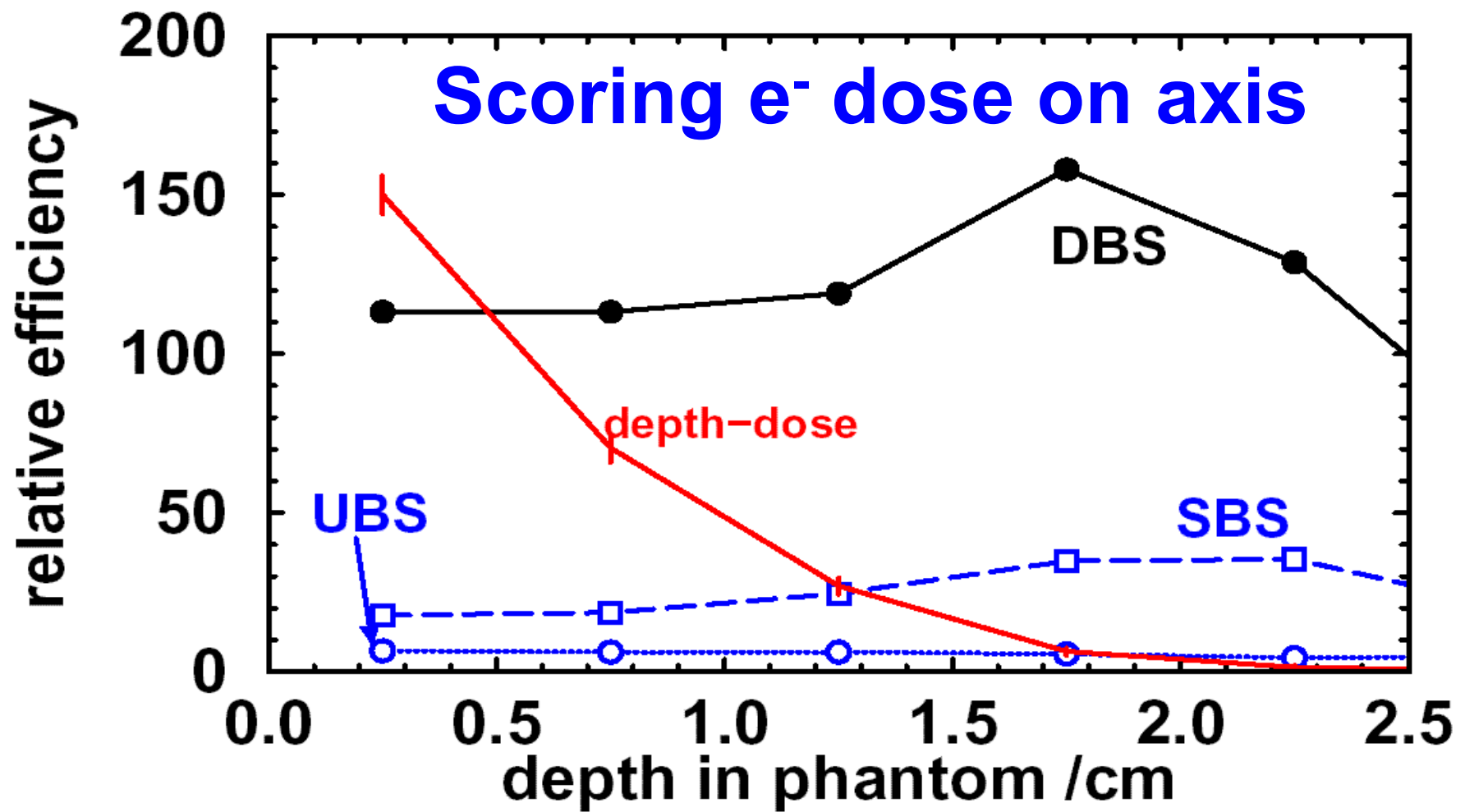
Electron solution

introduce 2 planes

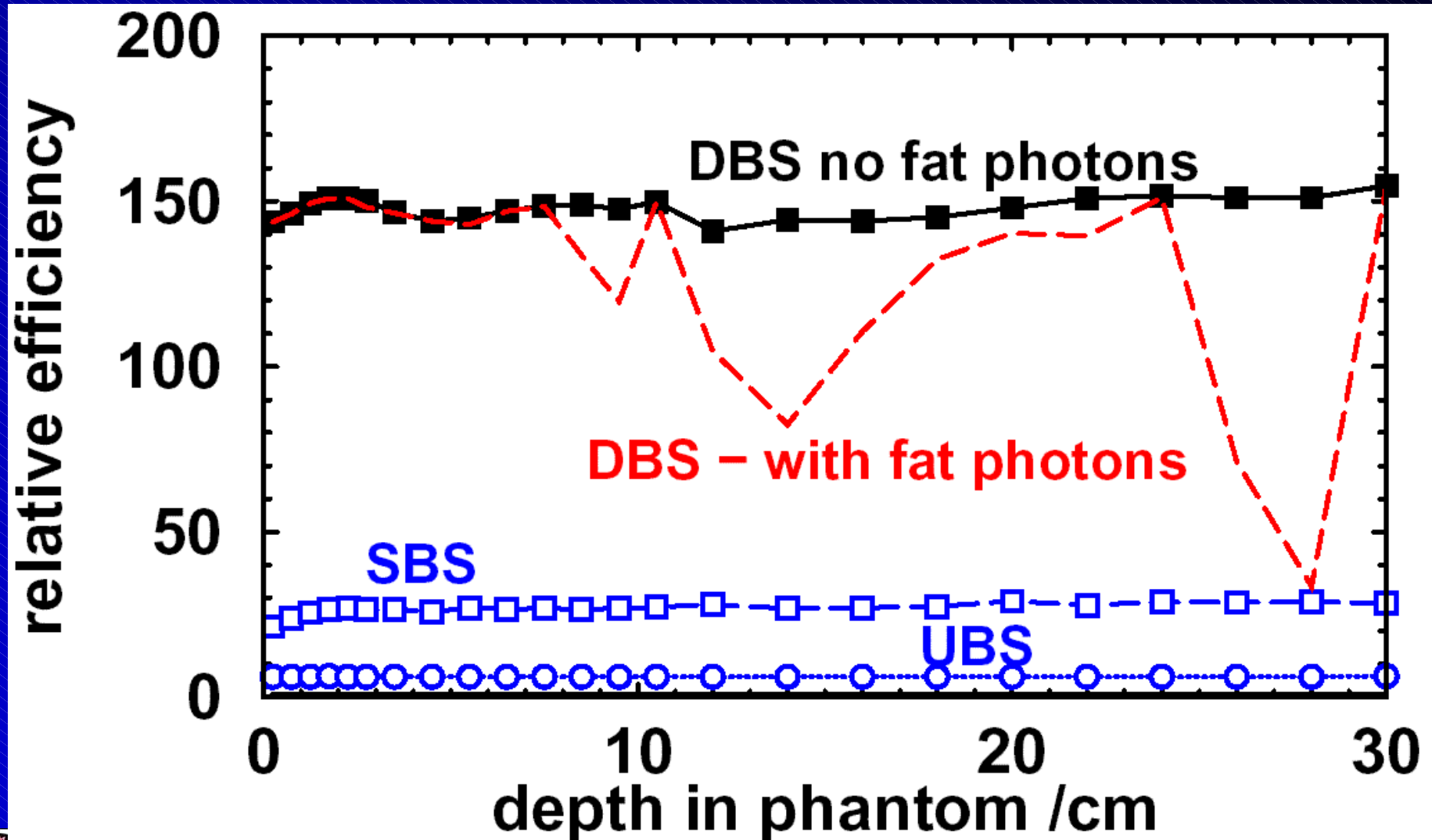
-**splitting plane**: split weight 1 charged particles **nsplit** times (may distribute symmetrically)

-**Russian roulette plane**: below this turn off **Russian roulette** and split all fat photon interactions **nsplit** times

Efficiency increase for e^-



Efficiency: total dose



Summary re DBS

DBS, directional brem splitting, improves BEAMnrc's efficiency by a factor of 800 (10 vs SBS) for photon beams (ignore small dose from photons outside field).

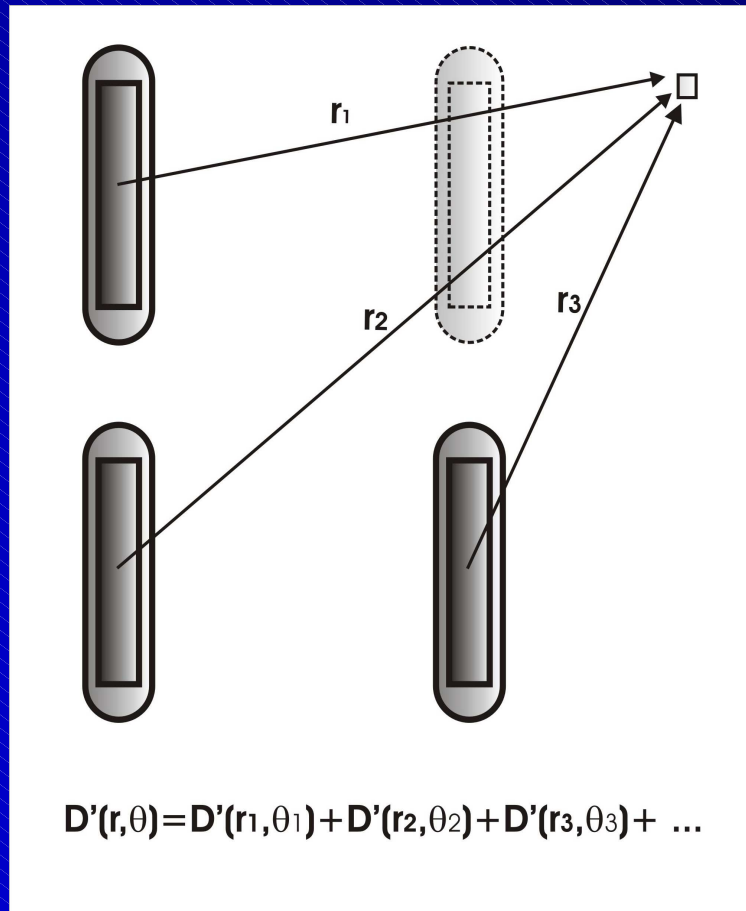
For total dose calculations the efficiency improves by factor of 150 (5 vs SBS)

SBS is optimized for greater nsplit than previously realized (5000)

Monte Carlo for brachytherapy dose

- **Gultekin Yegin** of Turkey has developed the multi-geometry technique for EGSnrc (NIMB)
- we applied it to multiple seeds in a phantom
- using **tracklength scoring** improves efficiency by a **factor 20**
- complete calculation, 125 seeds in 1 mm^3 voxels takes **12 min** for 2% stats on a 2.4MHz P-IV
- code called brachydose
- **What is the effect of inter-seed shielding?**

Inter-seed effects in brachytherapy

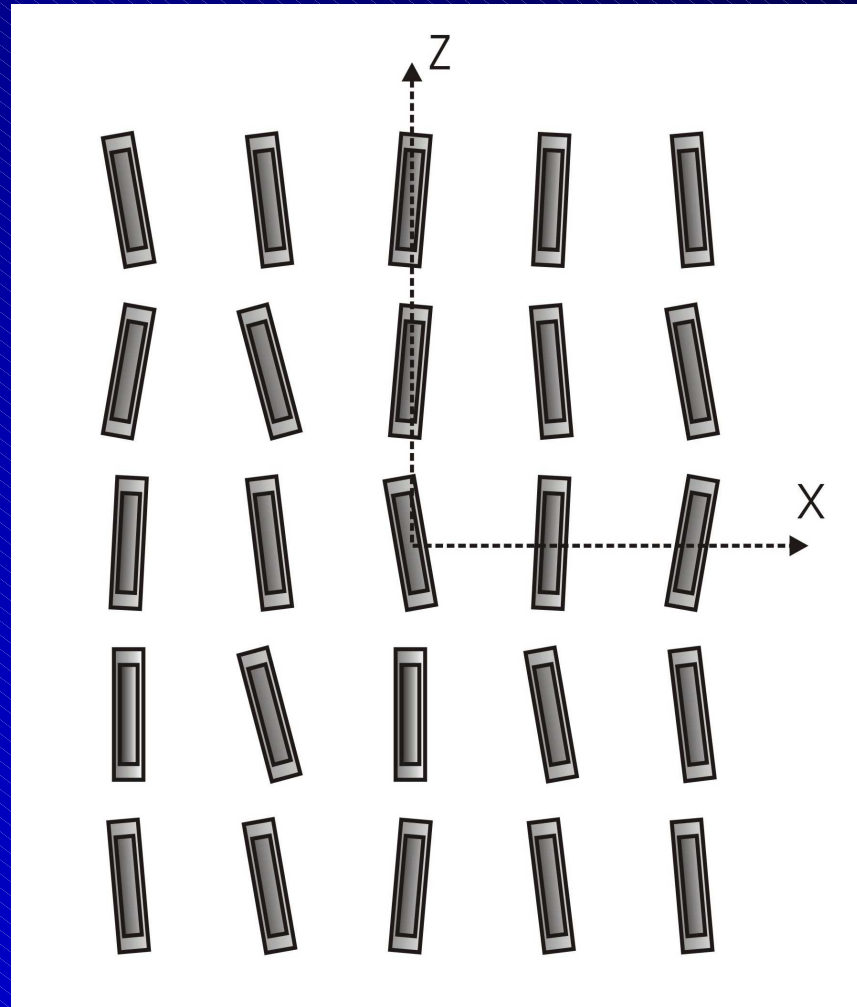


Standard planning systems ignore self-shielding

Only a few papers have investigated inter-seed effects.

In those papers, a small number of seeds are used in fixed configurations

Rotations of seeds



5 layers
deep

125 seeds

Dose perturbation factor

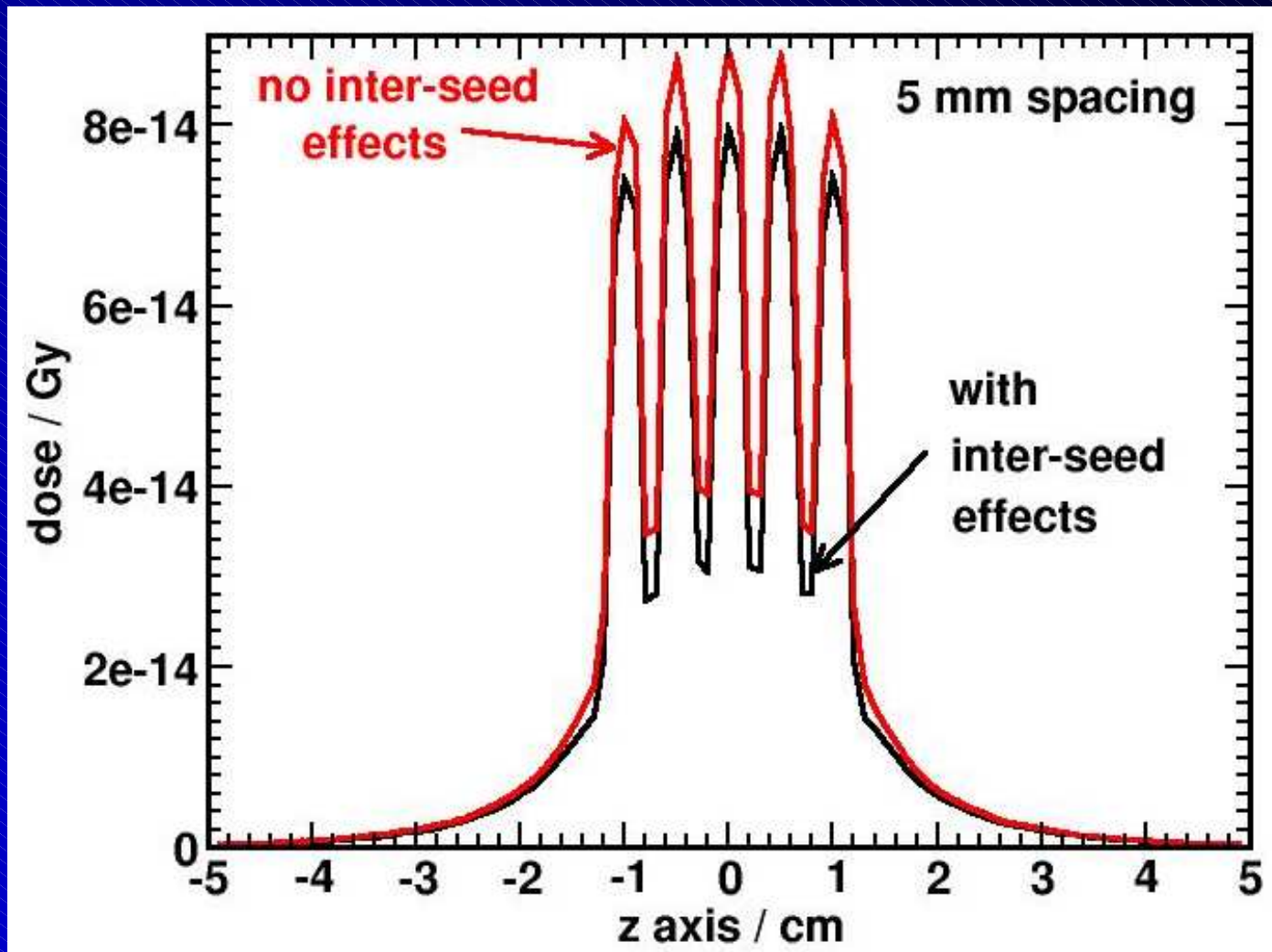
$$P = 100 \times [D(r, \theta) - D'(r, \theta)] / D(r, \theta)$$

P : Dose perturbation factor

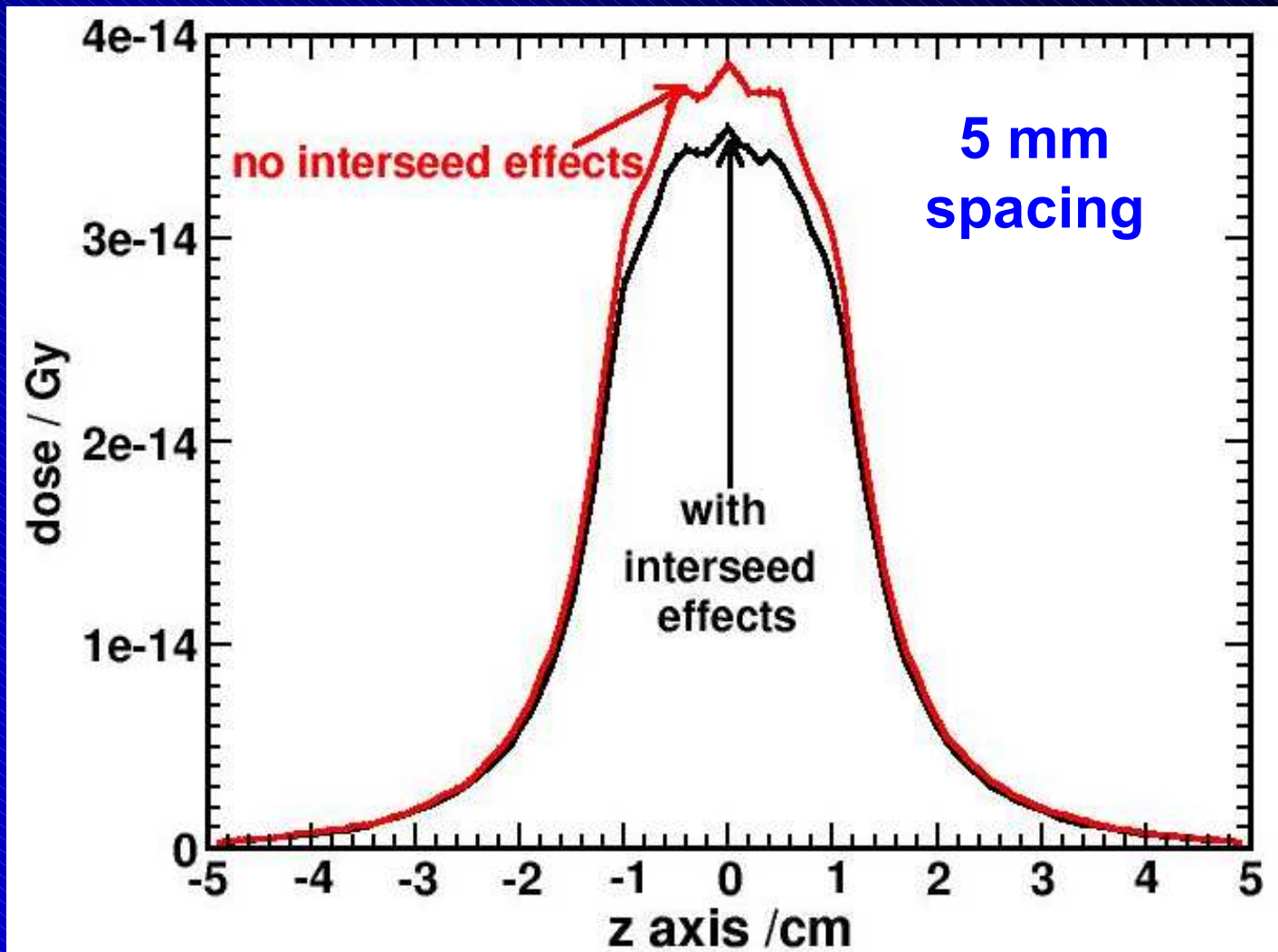
D : calculation with all **inter-seed effects included**

D' : calculation with all seeds (except that emitting the photon) **treated as water**

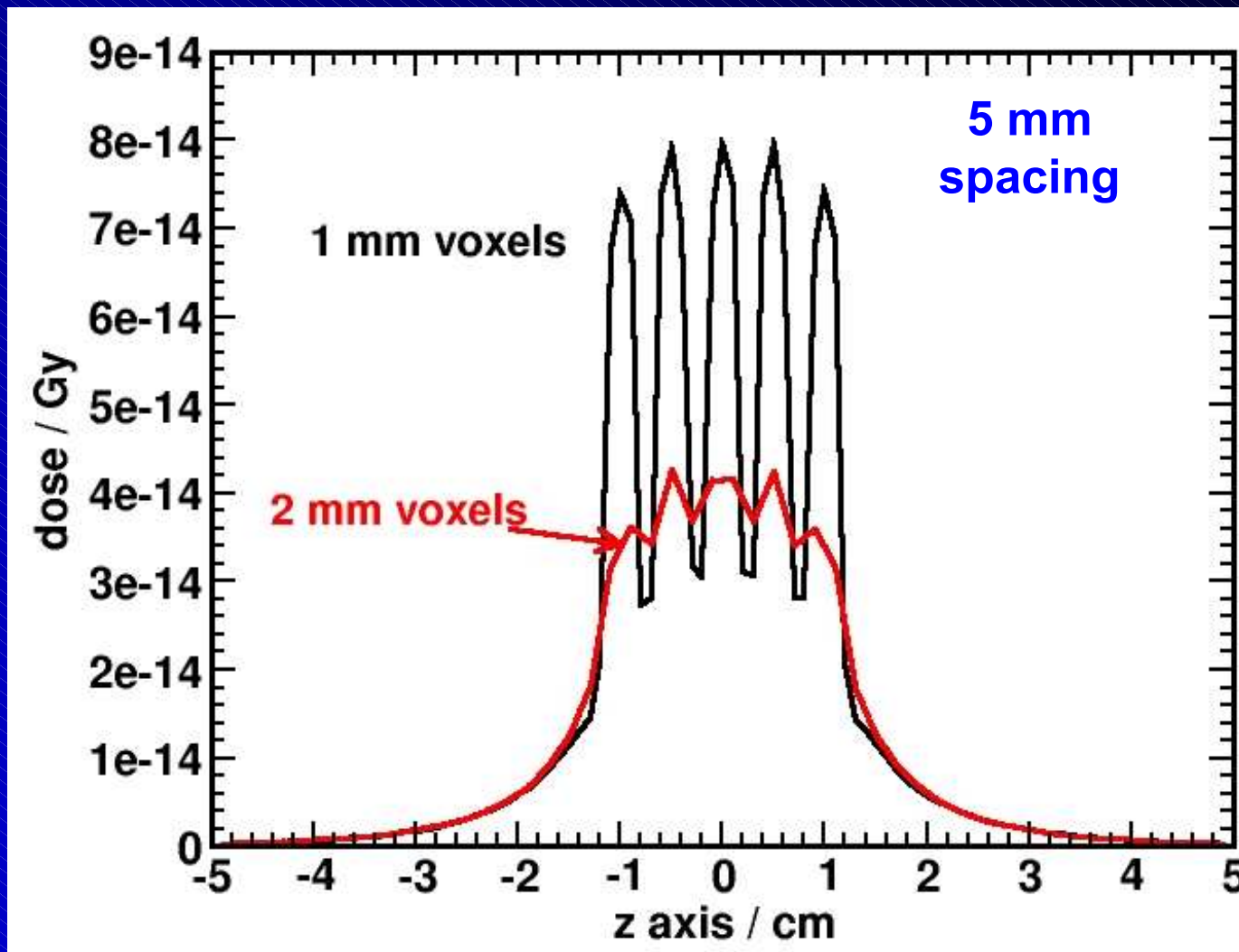
central axis dose for 5mm spacing



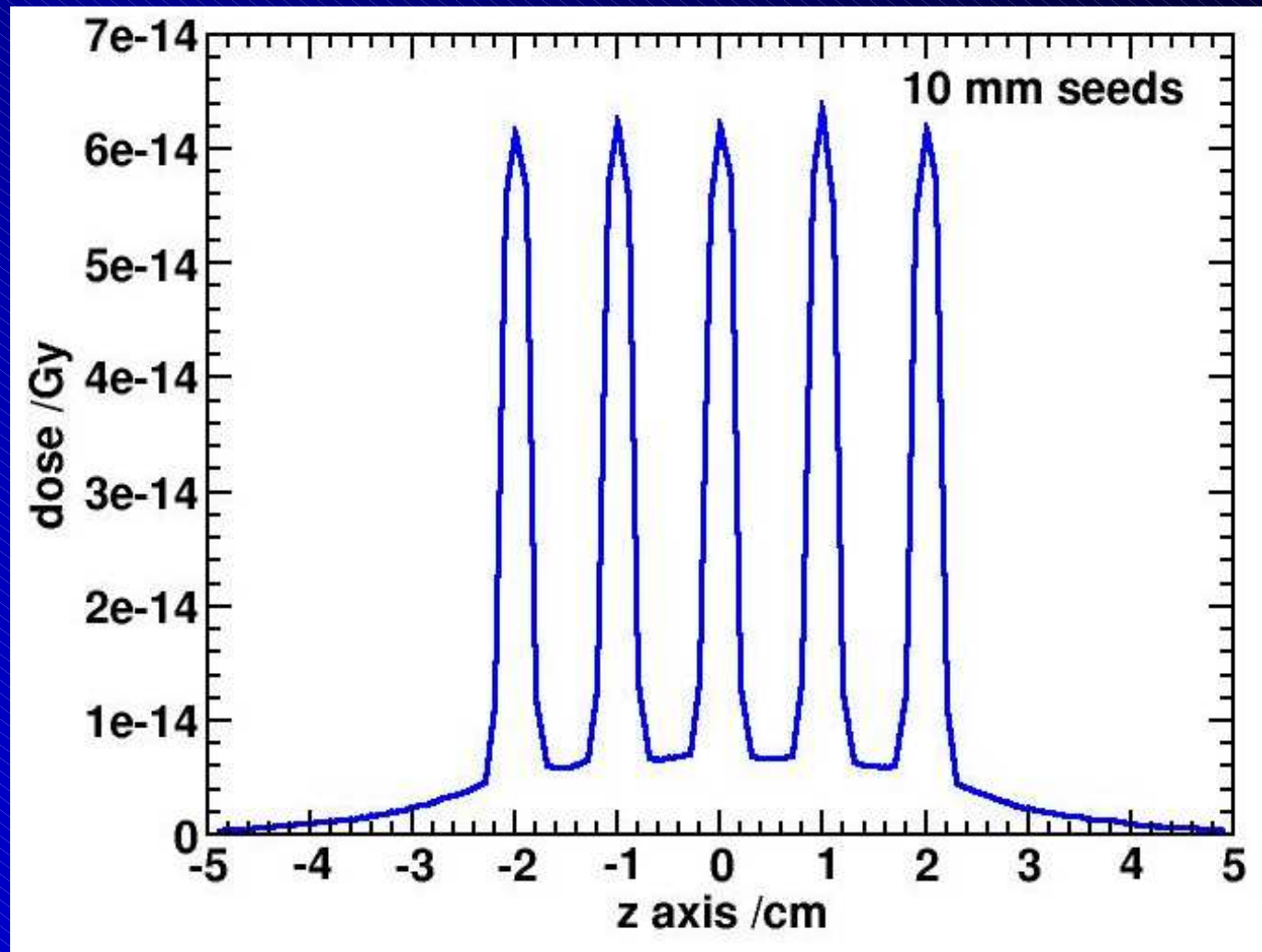
Dose on a line close to central axis



Influence of voxel size



10 mm spacing \Rightarrow 9 to 1 ratio



Summary re brachydose

- calculated dose perturbation factors are
 - 3% to 8% for 1 cm spacing of seeds
 - 4% to 30% for 0.5 cm spacing
- Using 1x1x1 mm voxel size, calculation of a dose distribution with 2% statistical uncertainty takes about 12 minutes on a pentium-4 2.4GHz cpu
 - expect a factor of 2 faster
- we hope to develop a generally available, clinically useful, code

Kawrakow's EGSnrc

Accurate condensed history Monte Carlo simulation of electron transport.

I. EGSnrc, the new EGS4 version

I. Kawrakow

National Research Council, Ottawa, ON K1A 0R6, Canada

(Received 10 March 1999; accepted for publication 8 December 1999)

485 Med. Phys. 27 (3), March 2000

Accurate condensed history Monte Carlo simulation of electron transport.

II. Application to ion chamber response simulations

I. Kawrakow

National Research Council, Ottawa, ON K1A 0R6, Canada

(Received 10 March 1999; accepted for publication 8 December 1999)

499 Med. Phys. 27 (3), March 2000

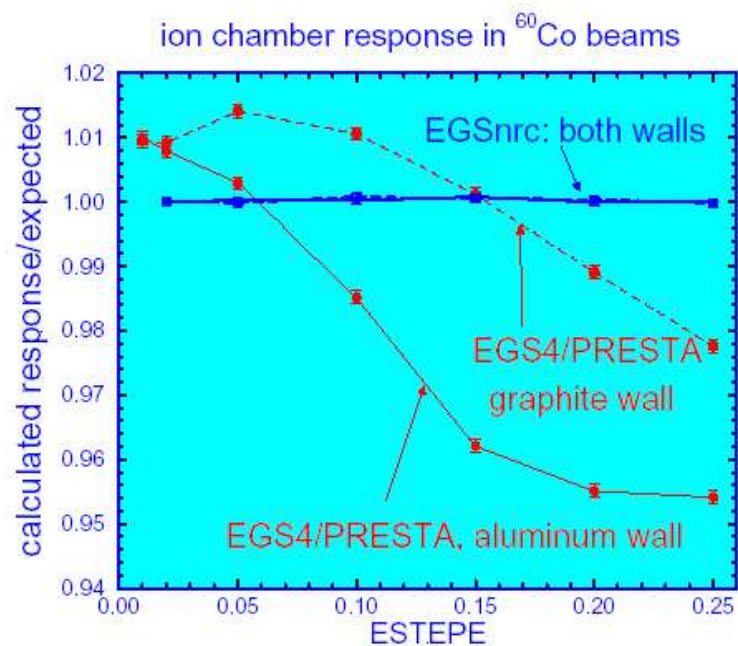
The EGSnrc Code System: Monte Carlo Simulation of Electron and Photon Transport

I. Kawrakow and D.W.O. Rogers

Ionizing Radiation Standards
National Research Council of Canada
Ottawa, K1A 0R6
iwan@irs.phy.nrc.ca
dave@irs.phy.nrc.ca

May 8, 2001

NRCC Report PIRS-701



Available on-line via:

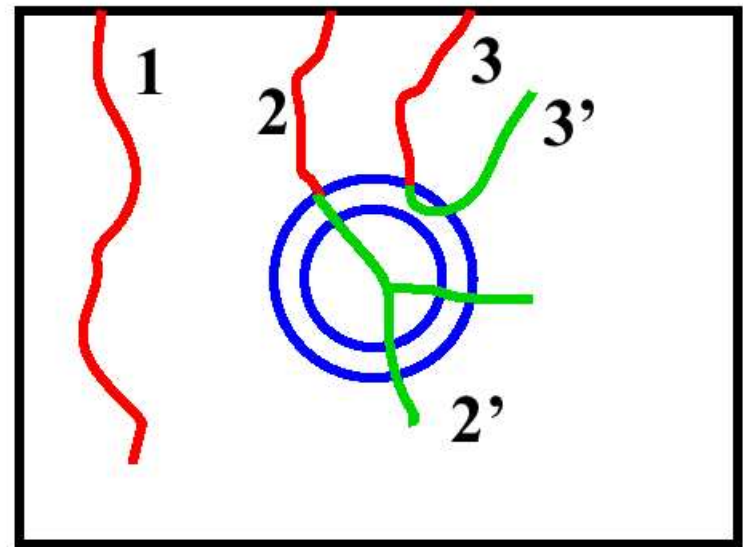
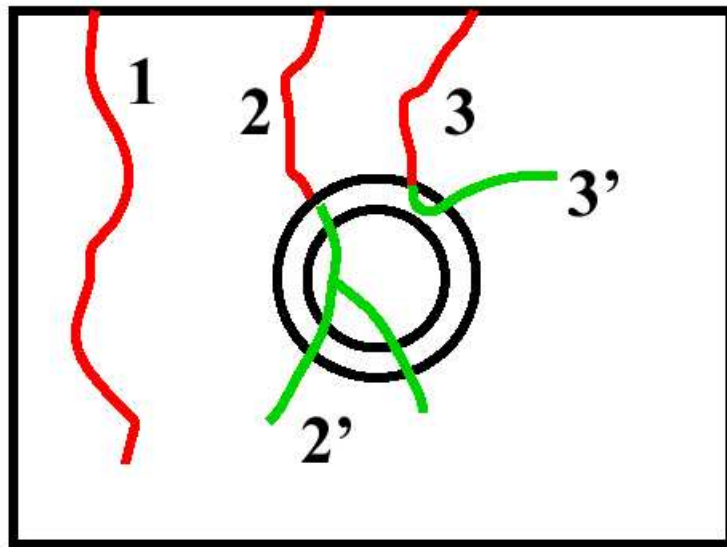
<http://www.irs.inms.nrc.ca/inms/irs/EGSnrc/EGSnrc.html>

©NRC Canada, 2001

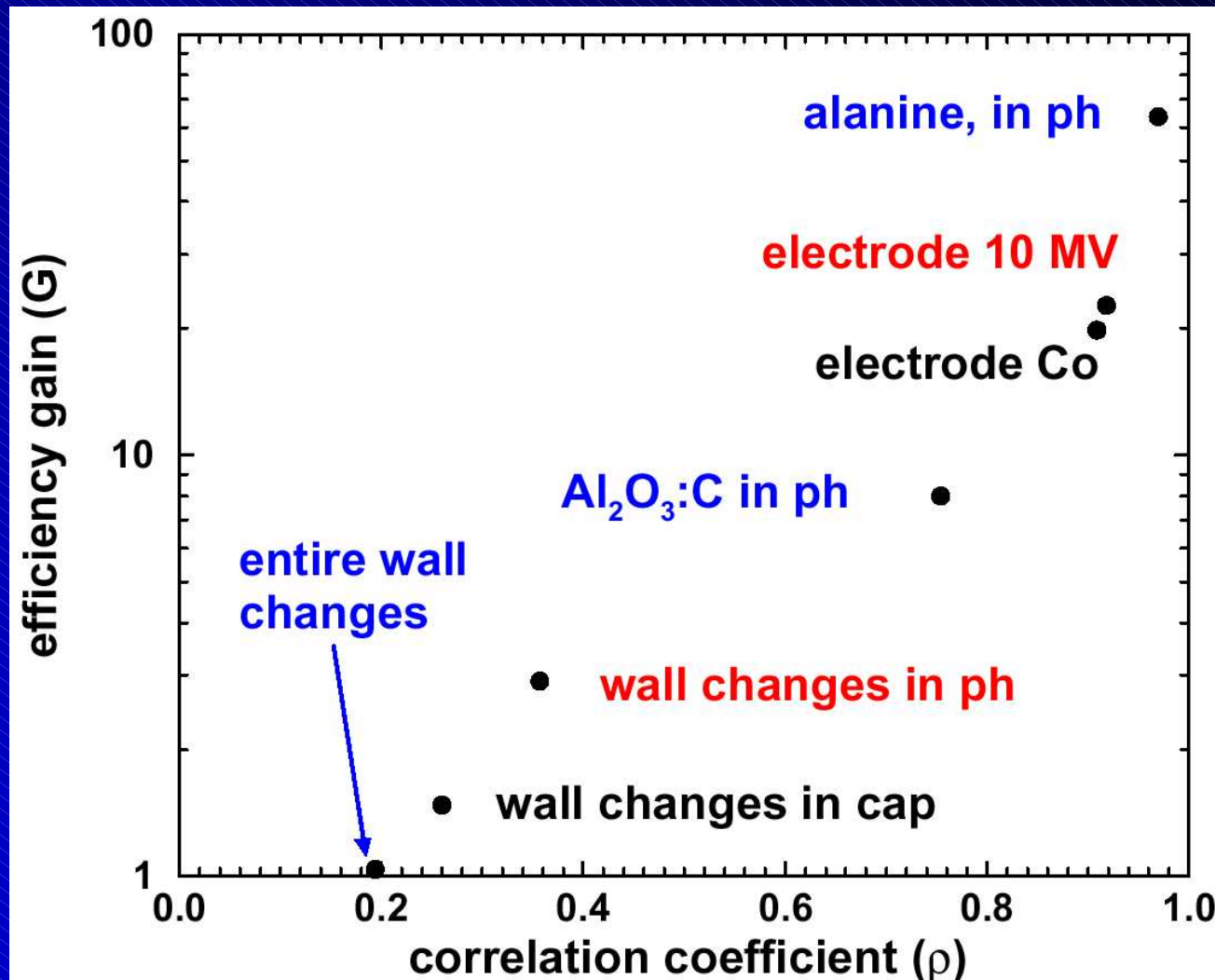
What is correlated sampling?

Of use when there are two or more similar geometries in which one wants the ratio of doses eg: electrodes, TLDs, wall effects, dosimeters in phantom, etc, etc

Originally developed by Ma and Nahum for EGS4



efficiency gain vs correlation



P_{cel} : Al electrode correction

-for electrode of wall material could be considered part of P_{fl}

Ma and Nahum(93) showed **aluminum electrodes** have an effect

-larger in **photon beams**

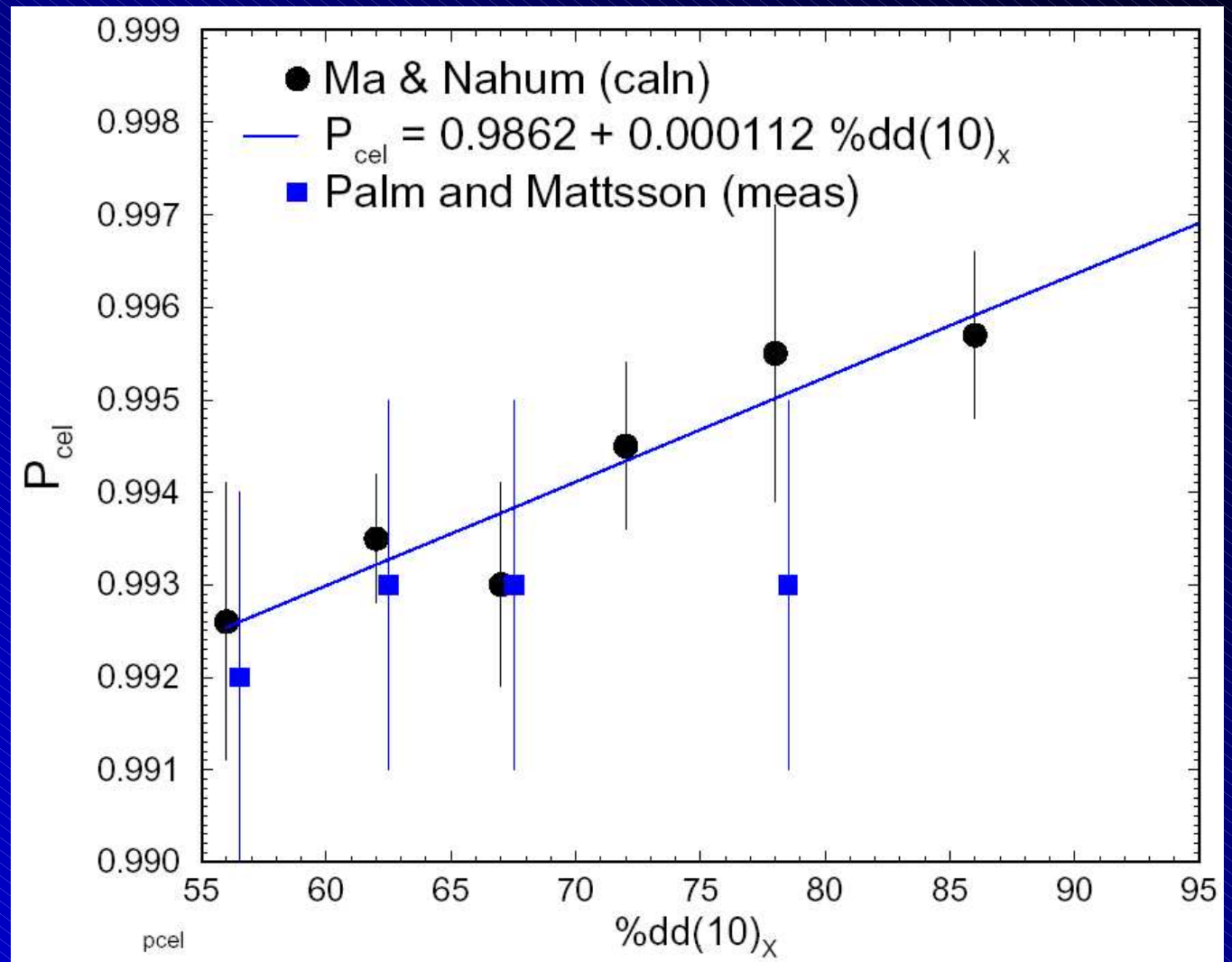
-but biggest effect is in **electron beams** because it cancels in photons

Ma & Nahum PMB 38 (1993) 267

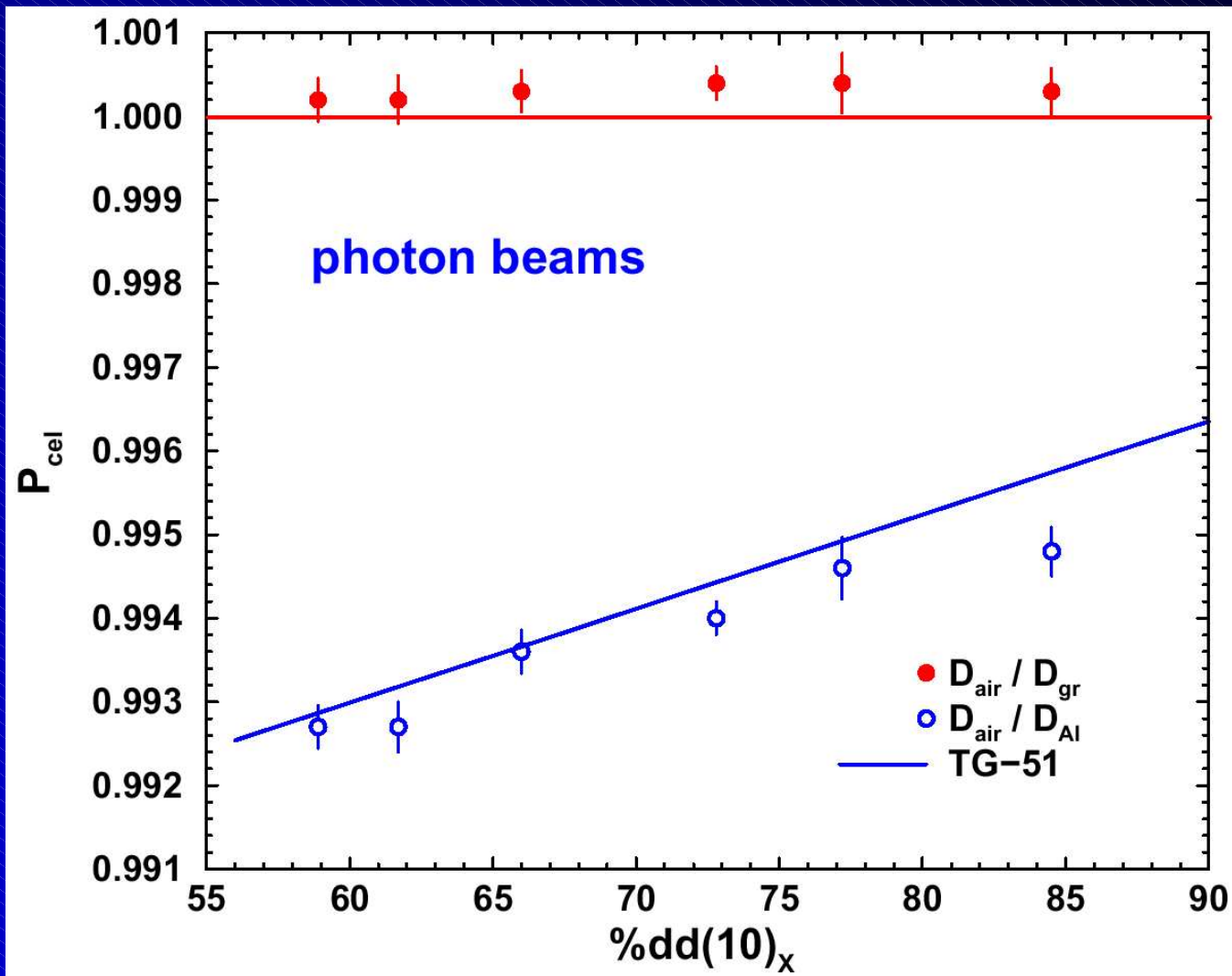
P_{cel} : Al electrode correction

-expts
confirm
calns

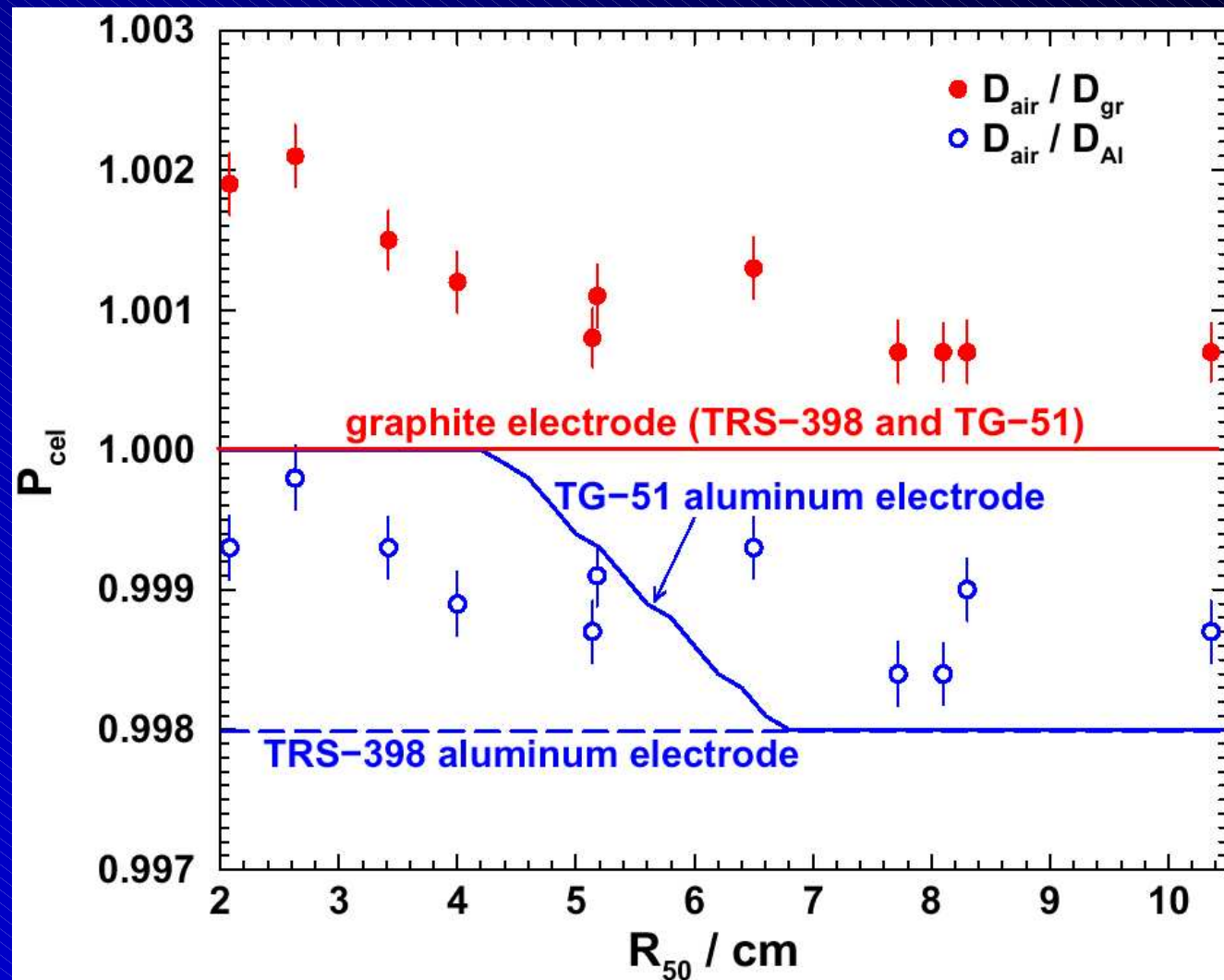
but not as
precise



New P_{cel} values for photon beams



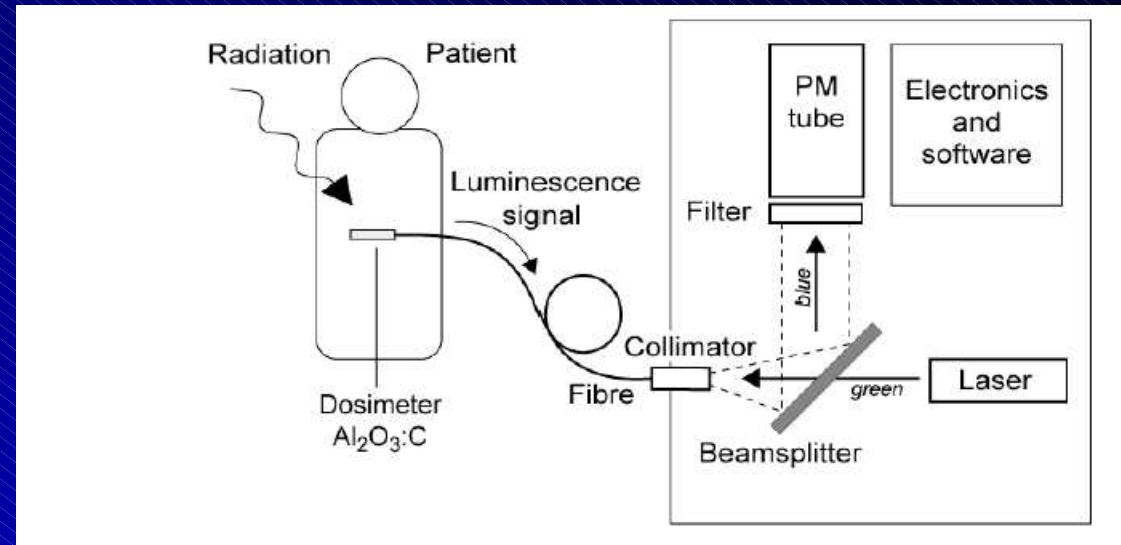
New P_{cel} values for electron beams



$\text{Al}_2\text{O}_3:\text{C}$ in radiation dosimetry

- uses **optically stimulated luminescence (OSL)**
- OSL uses a light source to stimulate luminescence
- signals from the dosimeter are relayed via a 1 mm core diameter fiber optic cable

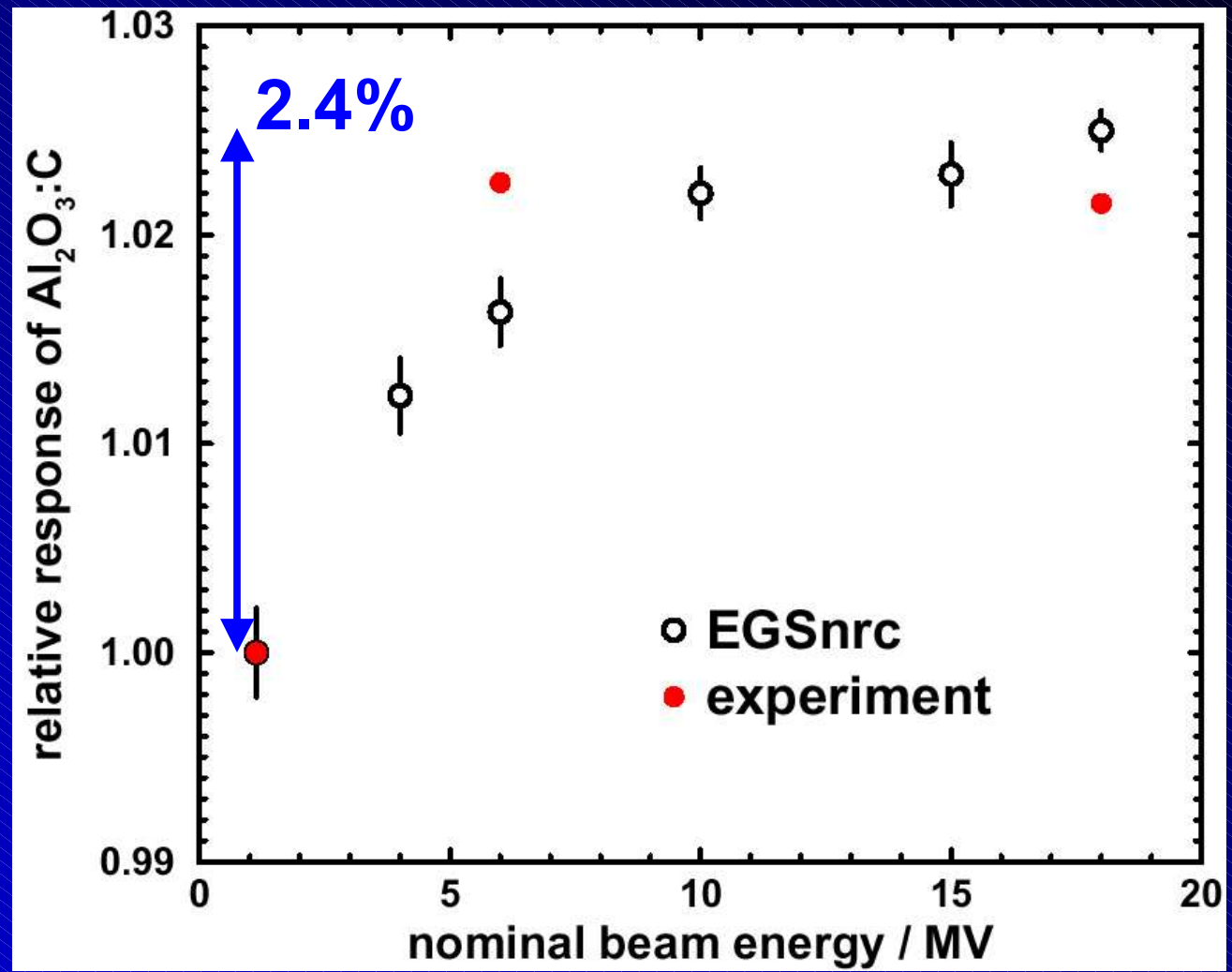
$\text{Al}_2\text{O}_3:\text{C}$ in radiation dosimetry



- small size detector (1 mm^3 or 2 mm^3)
- sensitive over a wide range of dose & dose rates
- can measure both dose and dose rate in real time

OSL calculations vs measurement

Results
normalized
at ^{60}Co
Preliminary
experimental
uncertainty
estimate is
on the order
of 1.5%



SNOMAN -MC for SNO

- the Monte Carlo simulation of the SNO detector (**SNOMAN**) uses **EGS4** to simulate the slowing of electrons
 - this is critical in determining the light output
- recently a **discrepancy with the calibration data** has been removed by adding in a patch to include Mott scattering in the simulation
- comparisons with **EGSnrc** demonstrate that the **SNOMAN patch gets the right answer**

Conclusions

- Monte Carlo is useful
 - making dosimetry more accurate
 - improving radiotherapy
 - golden age ahead as machines and codes faster and more flexible
- the future will see modelling to the biological level, not just physical dose

Thanks to

- many, many colleagues who have helped develop the BEAM/EGS codes discussed: Kawrakow, Walters, Nelson, Ding, Faddegon, Ma, Zhang, Mackie, Bielajew, Sheikh-Bagheri, Proulx + many users reporting bugs (sometimes patches!)
- Gultekin Yegin for slides and collaborating on brachydose
- Lesley Buckley for her data on correlated sampling
- Jerry Battista for good slide of the stamp